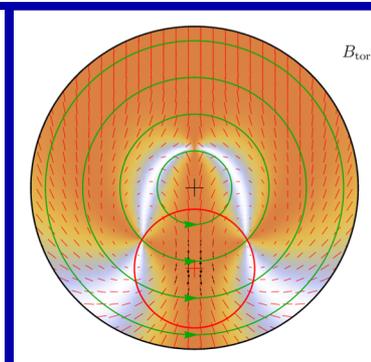
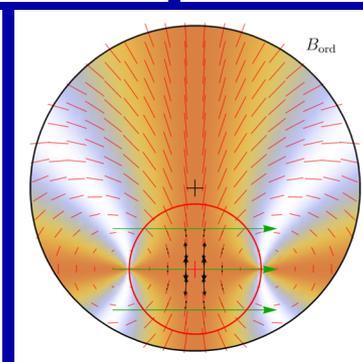
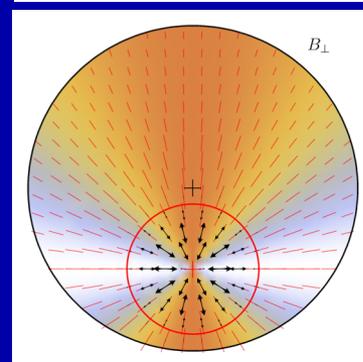
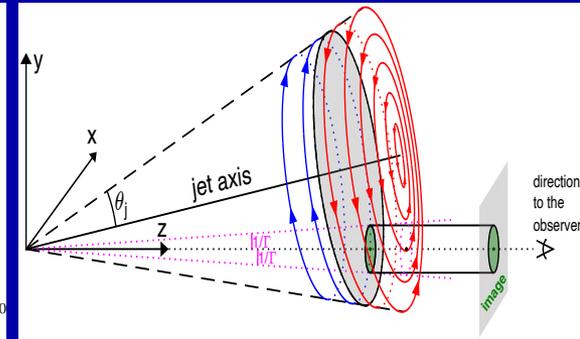
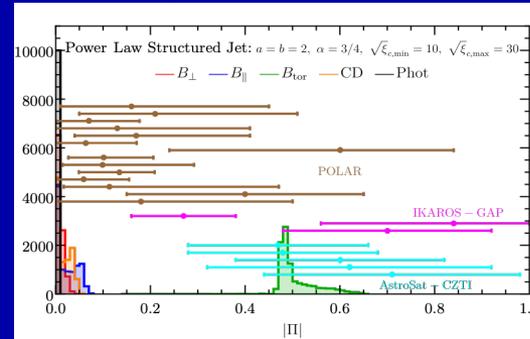
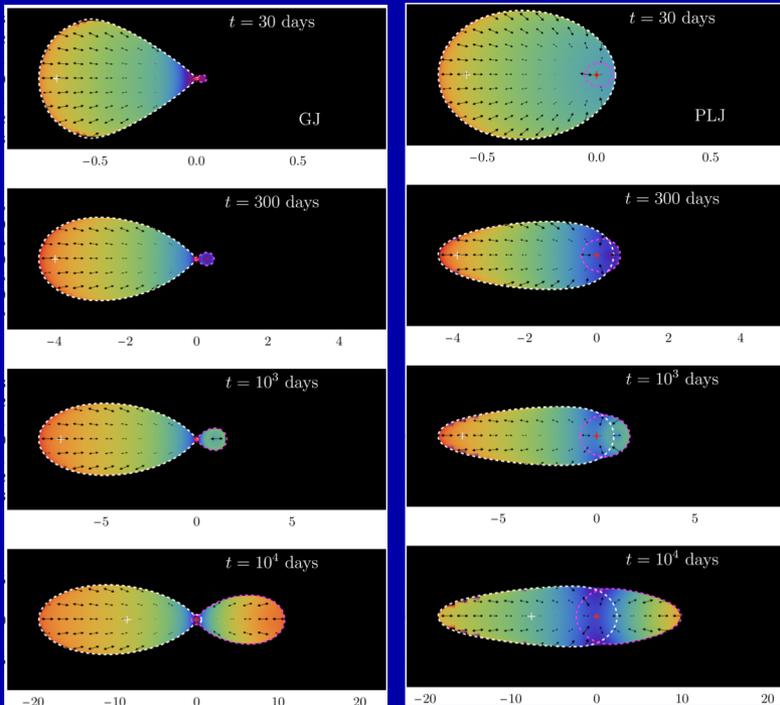


Gamma-Ray Burst Polarization: Status and Perspectives

Jonathan Granot

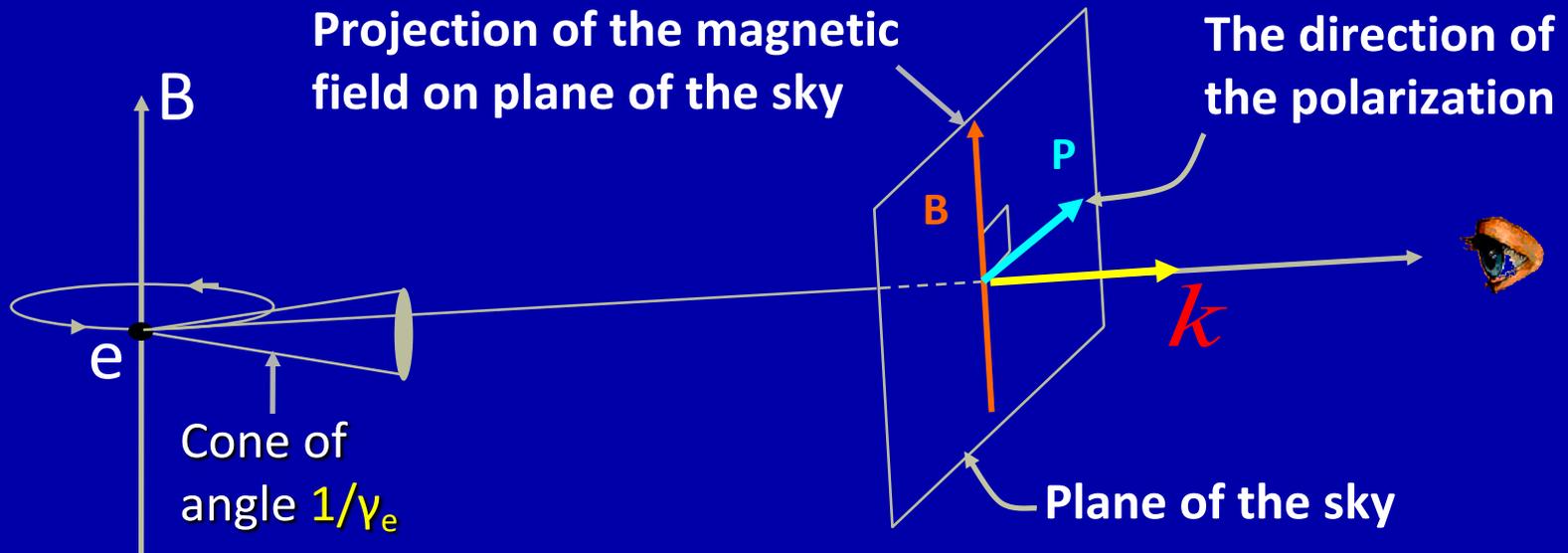
Open University of Israel & George Washington University

Collaborators: R. Gill, A. Königl, M. Kole, P. Kumar, T. Laskar



Astrophysical Polarimetry in the Time-Domain Era, Lecco, Italy, 1/9/22

Polarization of Synchrotron Emission

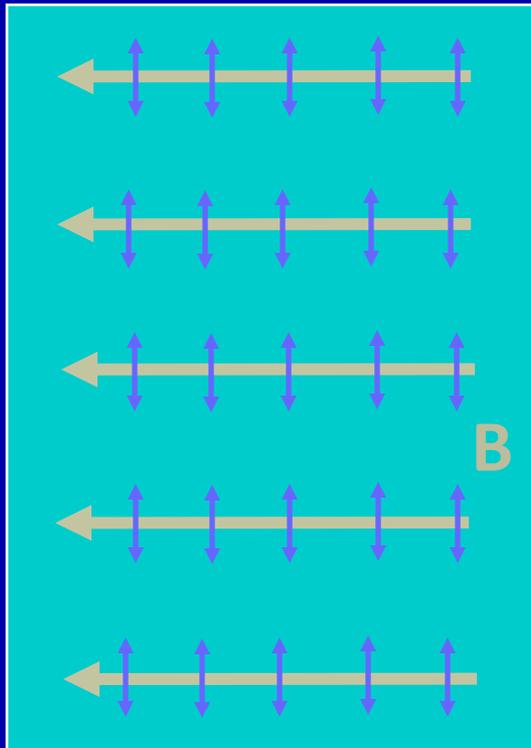


- **linear polarization** is perpendicular to the projection of **B** on the plane of the sky (normal to the wave vector)
- The maximal polarization is for the local emission from an ordered **B**-field: $P_{\max} = (\alpha+1)/(\alpha+5/3)$ where $F_\nu \propto \nu^{-\alpha}$, $-1/3 \leq \alpha \lesssim 1.5 \Rightarrow 50\% \leq P_{\max} \lesssim 80\%$
(Rybicki & Lightman 1979; Granot 2003)

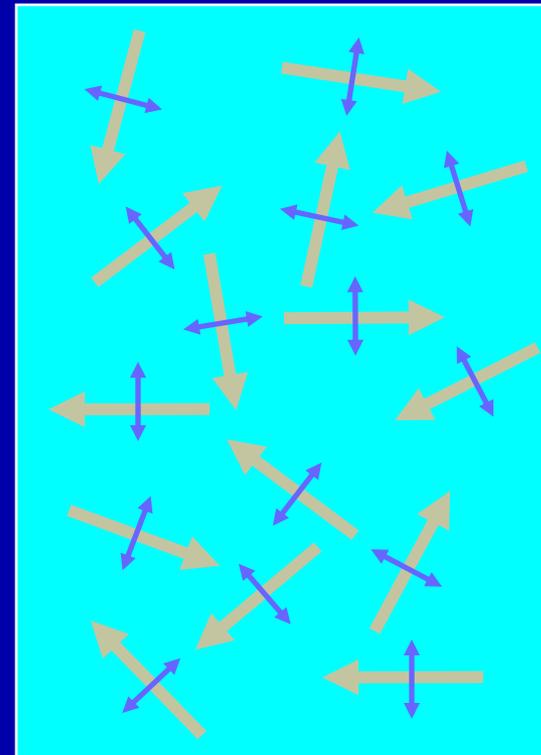
In the source rest frame:

- A uniform field produces $\mathbf{P} = \mathbf{P}_{\max}$
- For a field random when projected on the plane of the sky: $\mathbf{P} = \mathbf{0}$
- In particular, for a field isotropically tangled in 3D: $\mathbf{P} = \mathbf{0}$

Uniform B

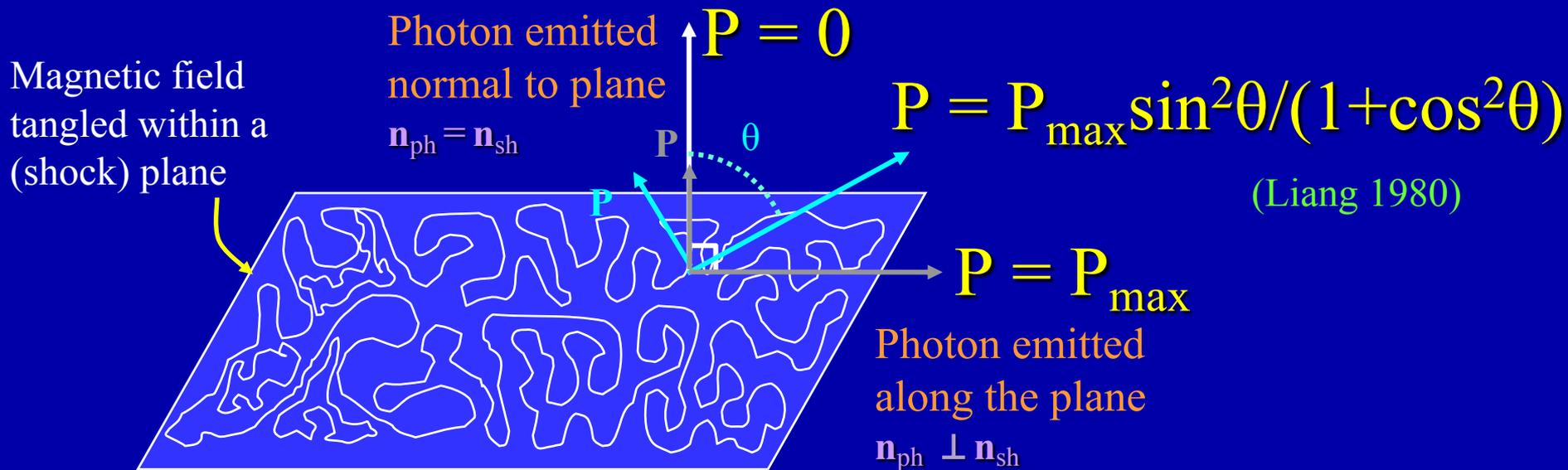


Random B

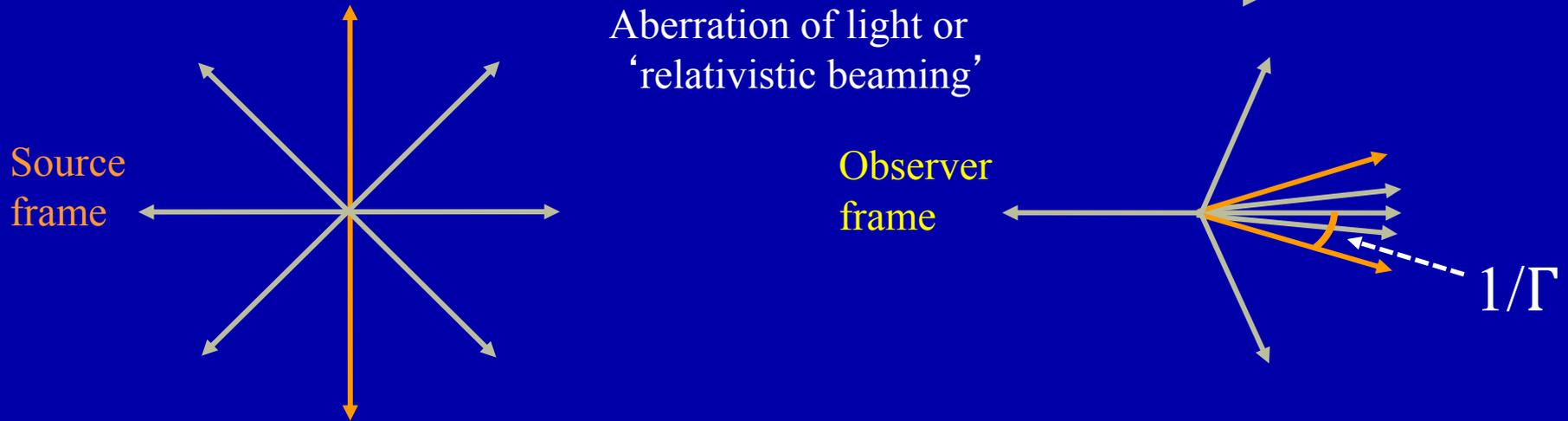


Shock Produced Magnetic Field:

- A magnetic field produced at a relativistic collisionless shock, due to the two-stream instability, is **naively** expected to be **tangled within the plane of the shock** (Medvedev & Loeb 1999)

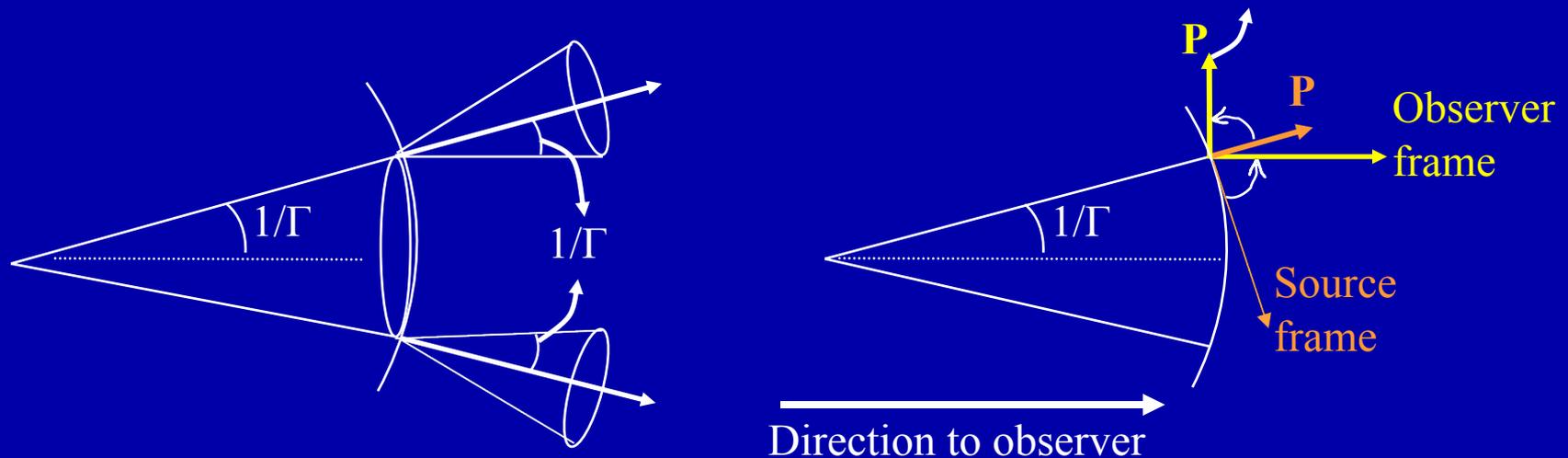


Relativistic source:



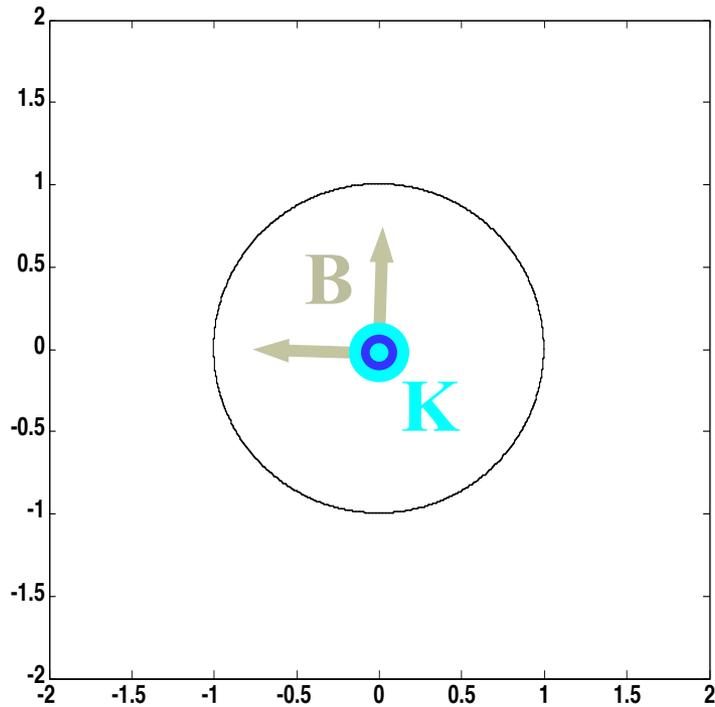
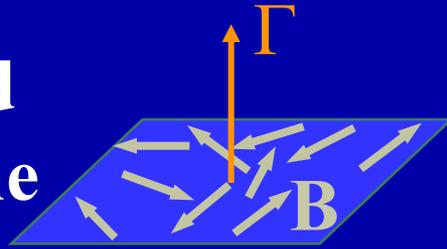
The observer sees mostly emission from within an angle of $1/\Gamma$ around the l.o.s.

Direction of Polarization



Polarization in the observer frame

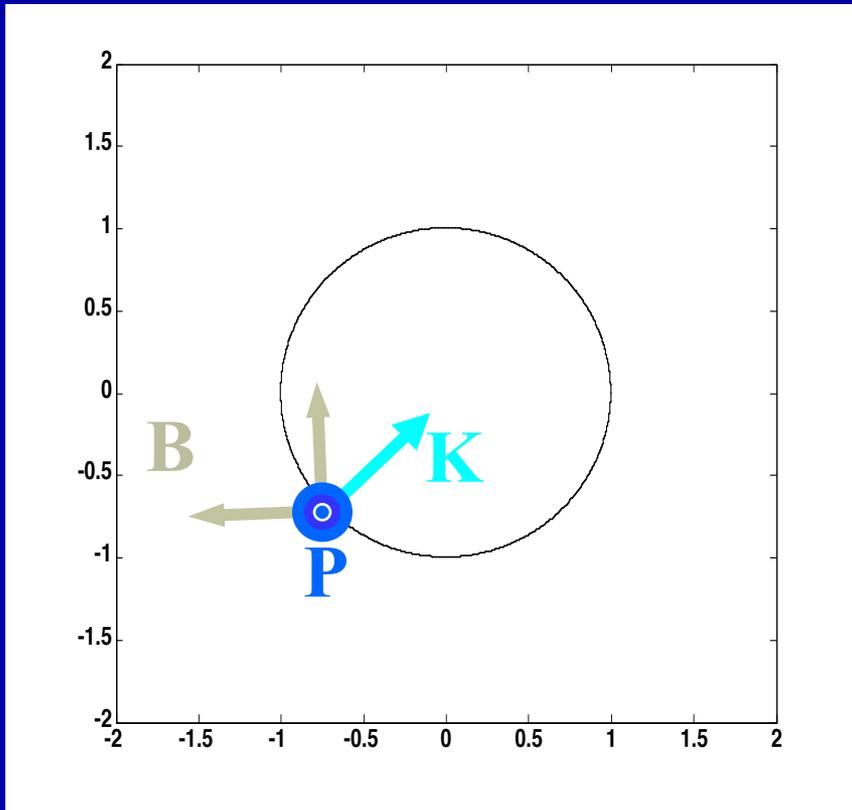
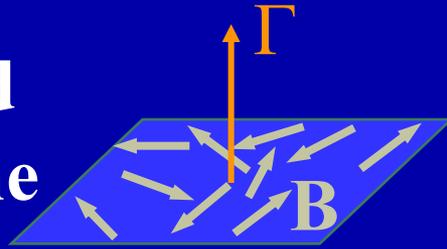
Random field
in shock plane



Sari 99; Ghisellini & Lazzati 99

Polarization in the observer frame

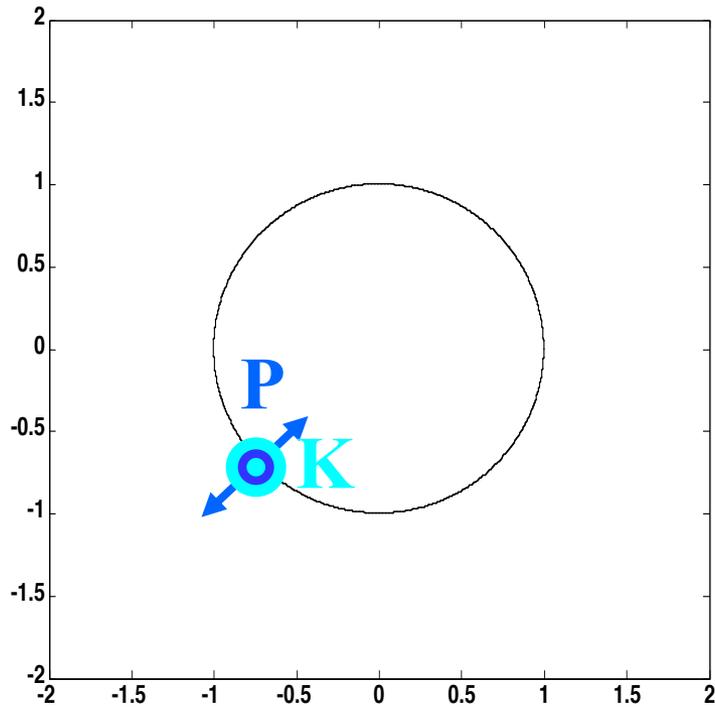
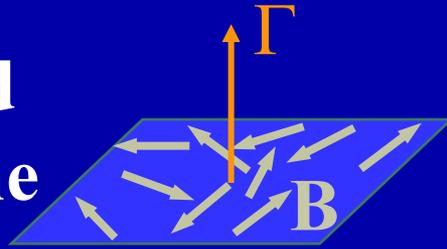
Random field
in shock plane



Sari 99; Ghisellini & Lazzati 99

Polarization in the observer frame

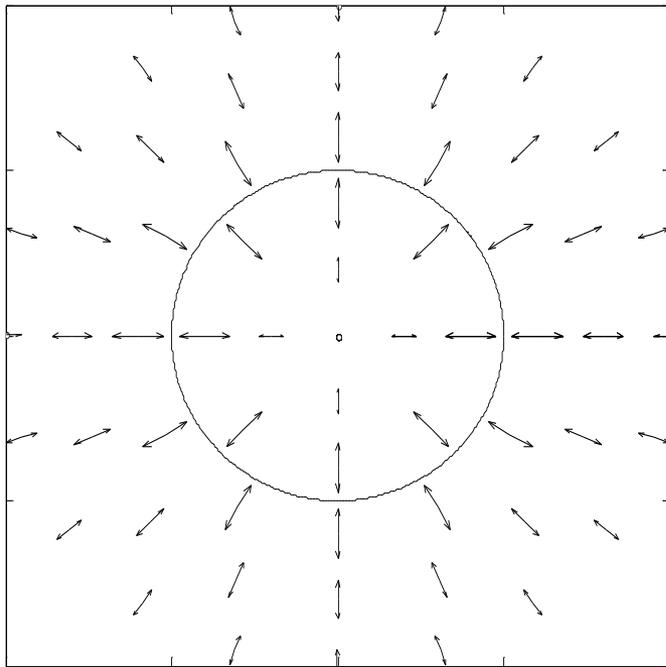
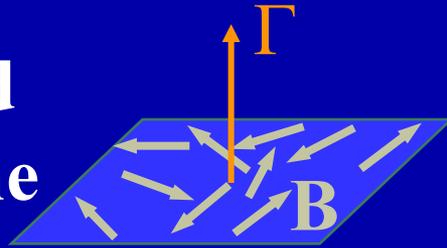
Random field
in shock plane



Sari 99; Ghisellini & Lazzati 99

Polarization in the observer frame

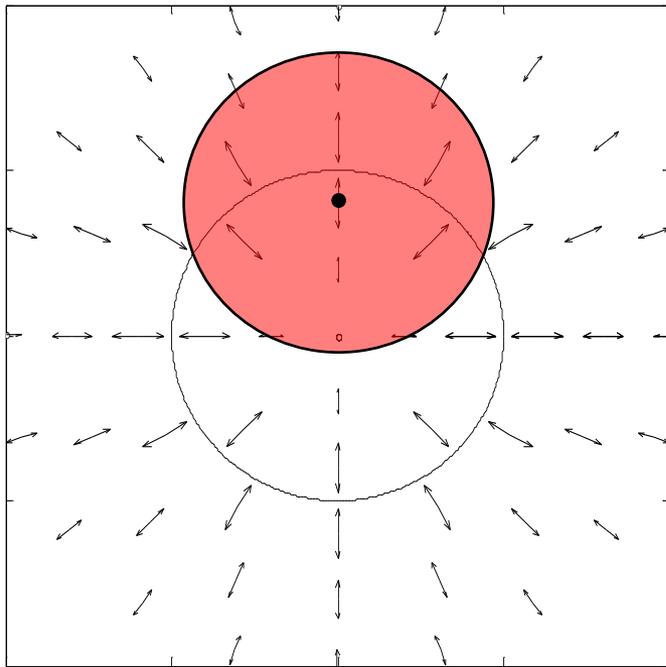
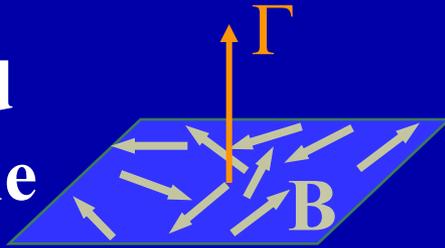
Random field
in shock plane



Sari 99; Ghisellini & Lazzati 99

Polarization in the observer frame

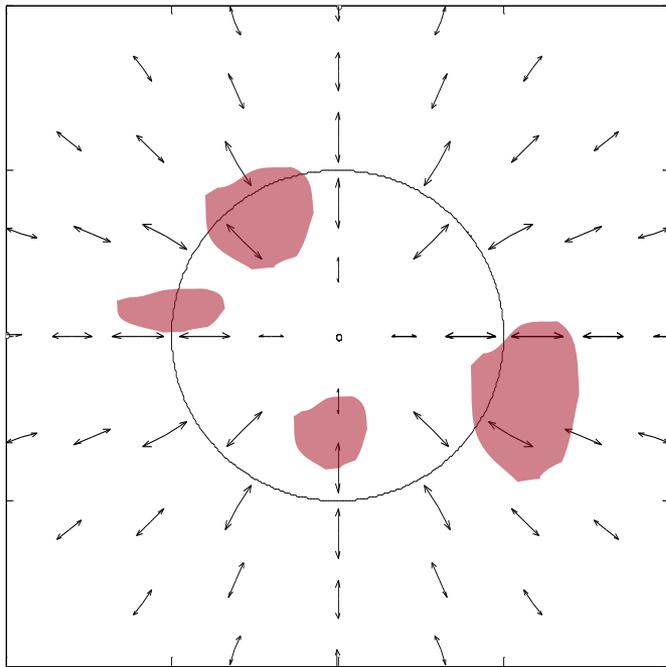
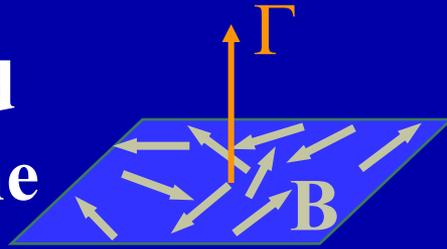
Random field
in shock plane



Sari 99; Ghisellini & Lazzati 99

Polarization in the observer frame

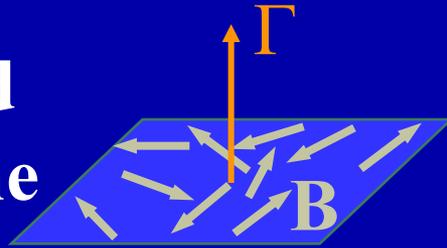
Random field
in shock plane



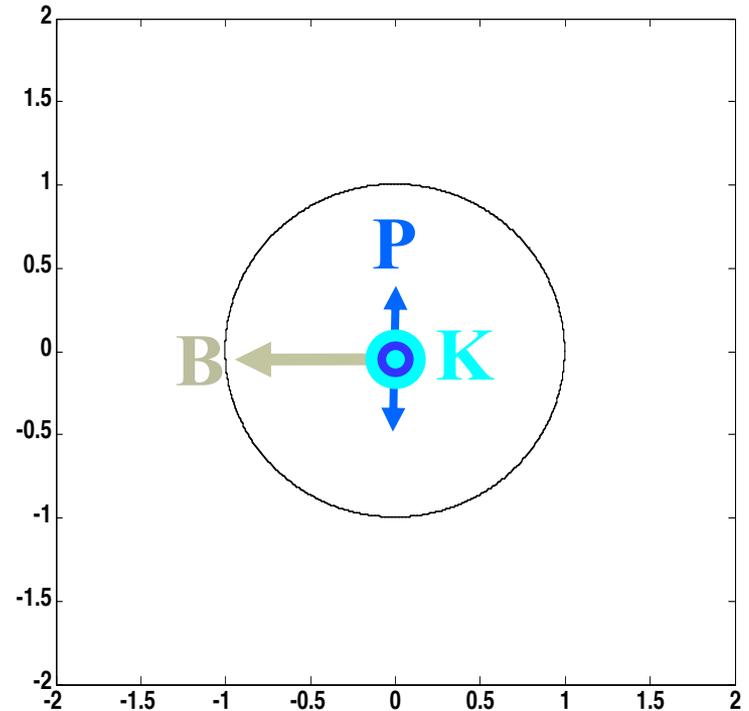
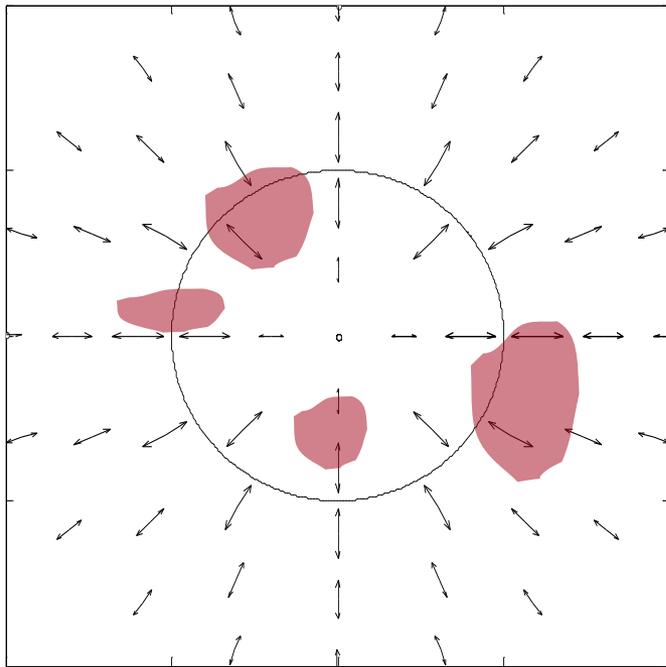
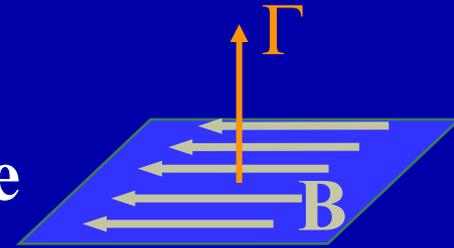
Sari 99; Ghisellini & Lazzati 99

Polarization in the observer frame

Random field
in shock plane



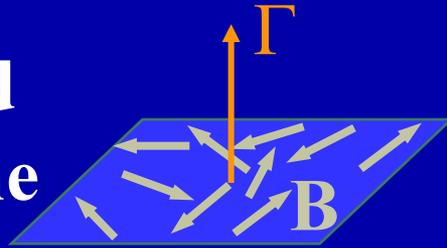
Ordered field
in shock plane



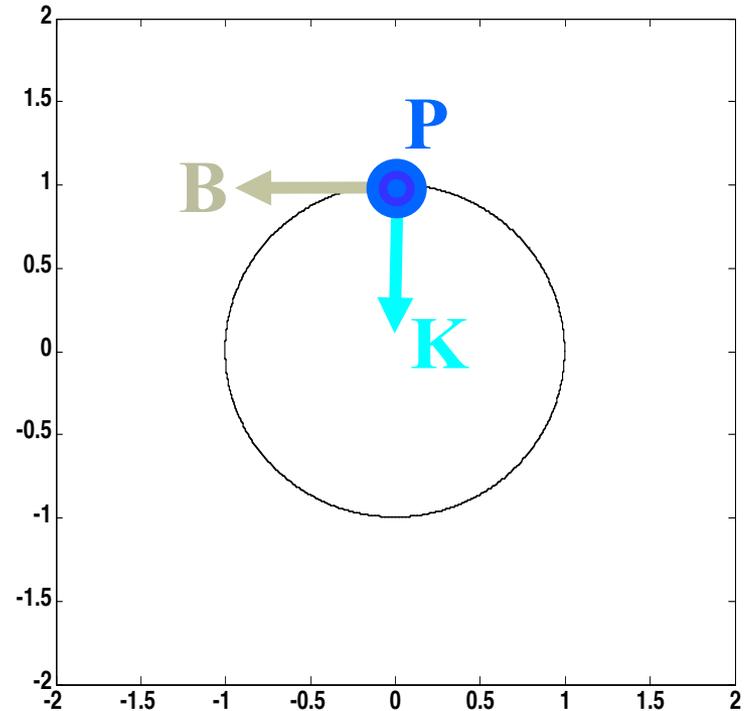
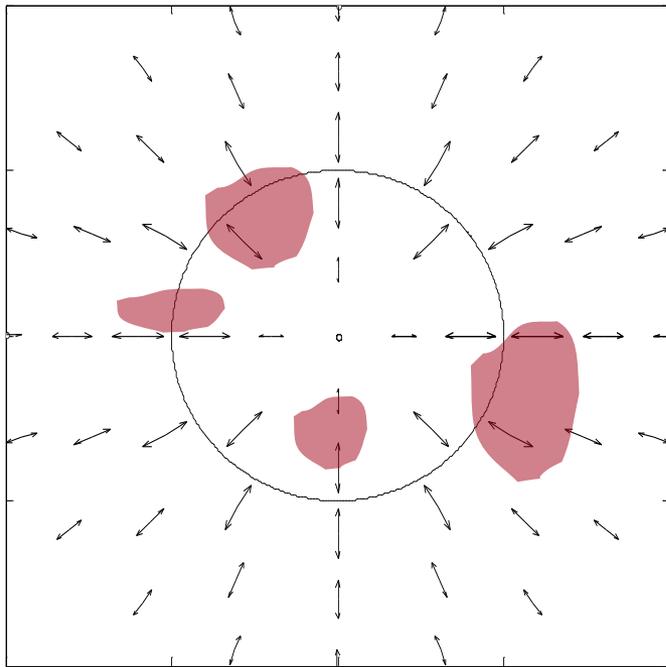
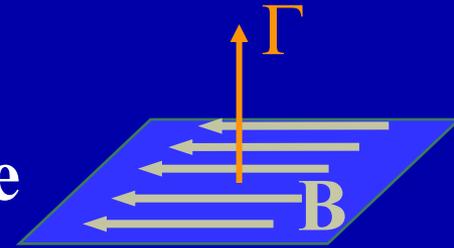
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Polarization in the observer frame

Random field
in shock plane



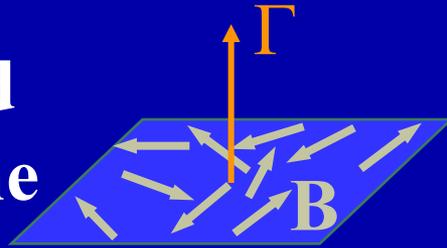
Ordered field
in shock plane



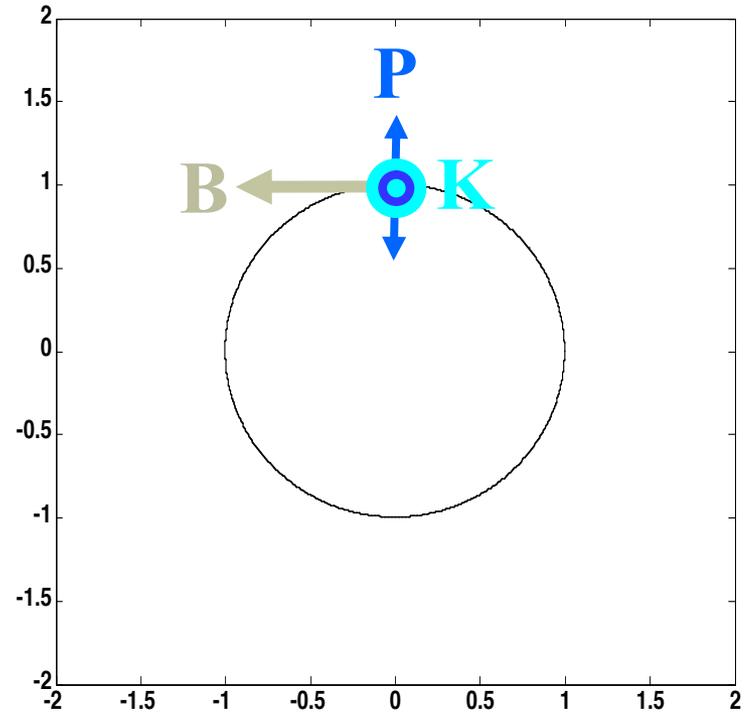
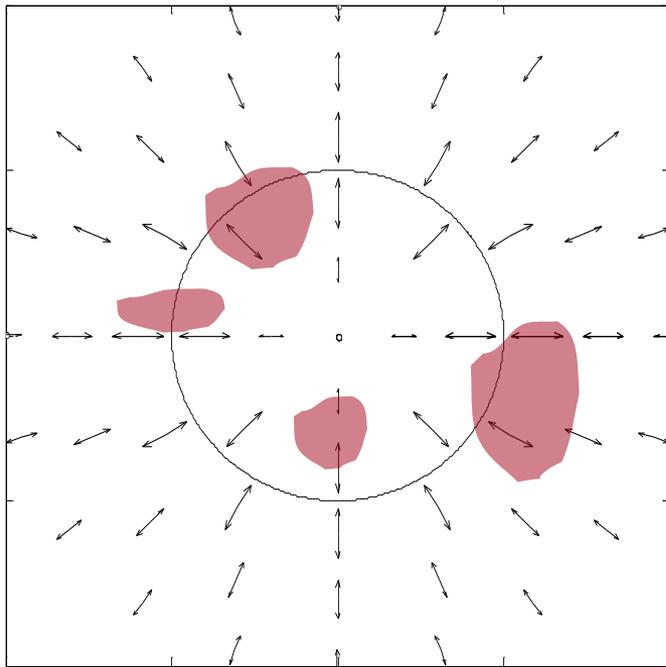
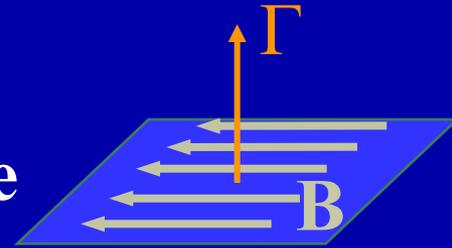
Sari 99; Ghisellini & Lazzati 99

Polarization in the observer frame

Random field
in shock plane



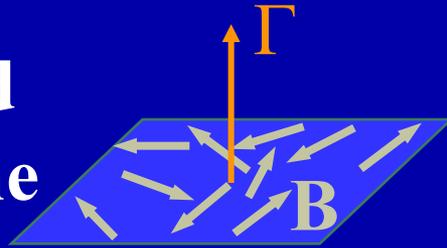
Ordered field
in shock plane



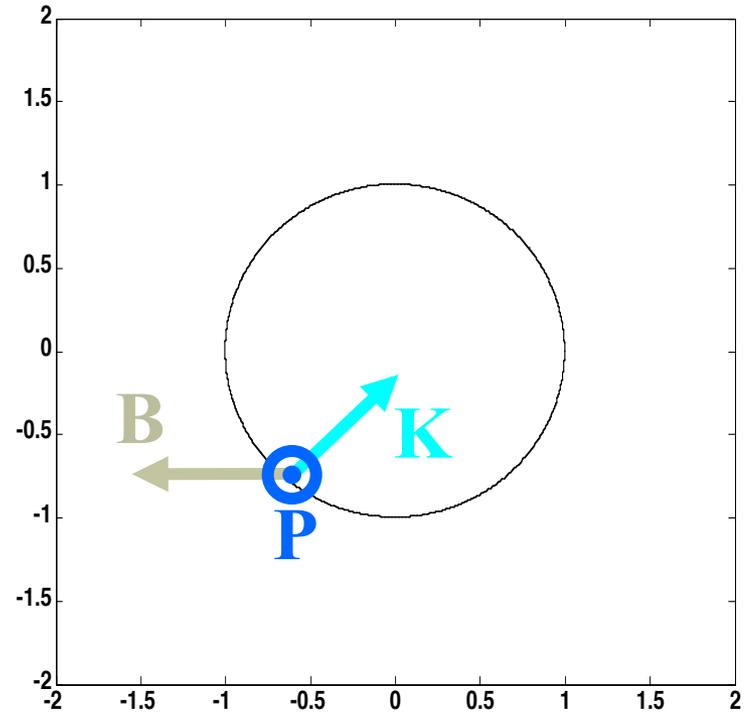
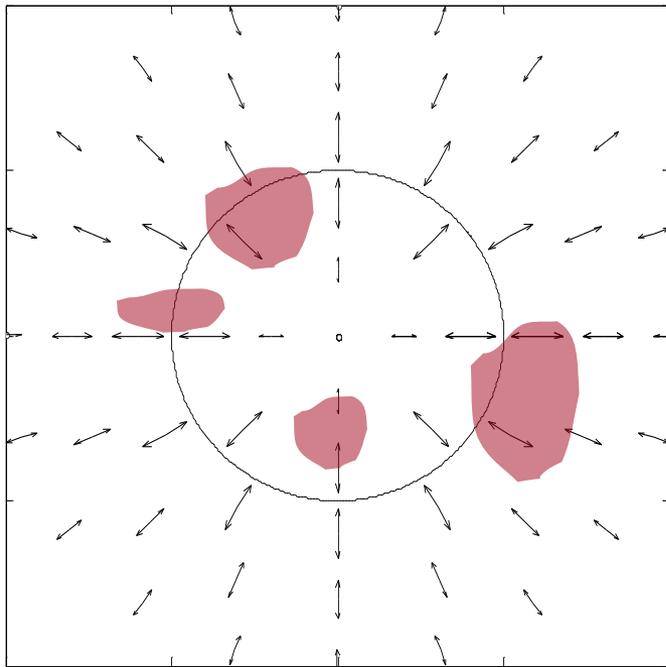
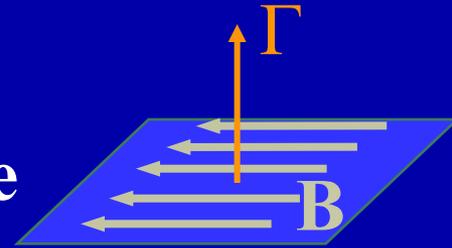
Sari 99; Ghisellini & Lazzati 99

Polarization in the observer frame

Random field
in shock plane



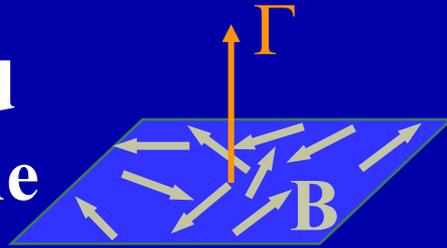
Ordered field
in shock plane



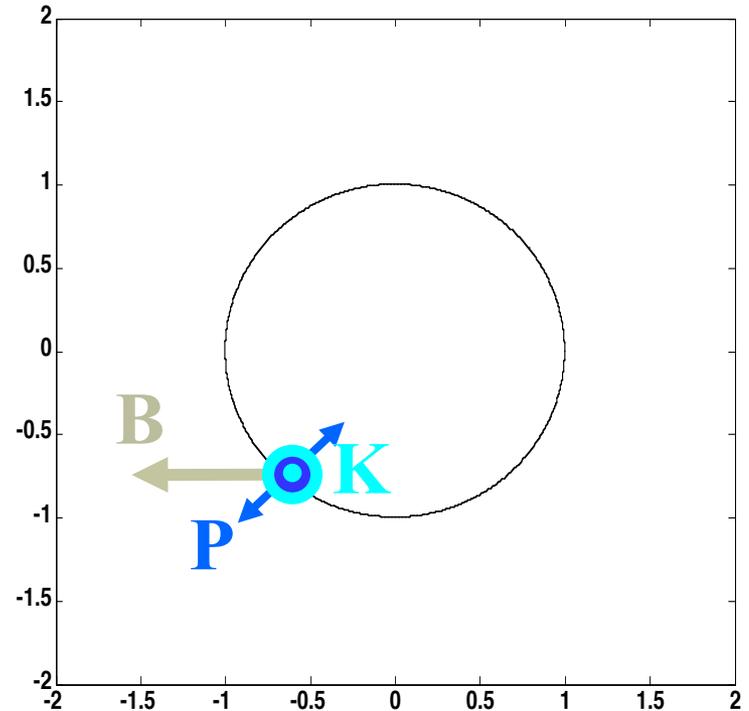
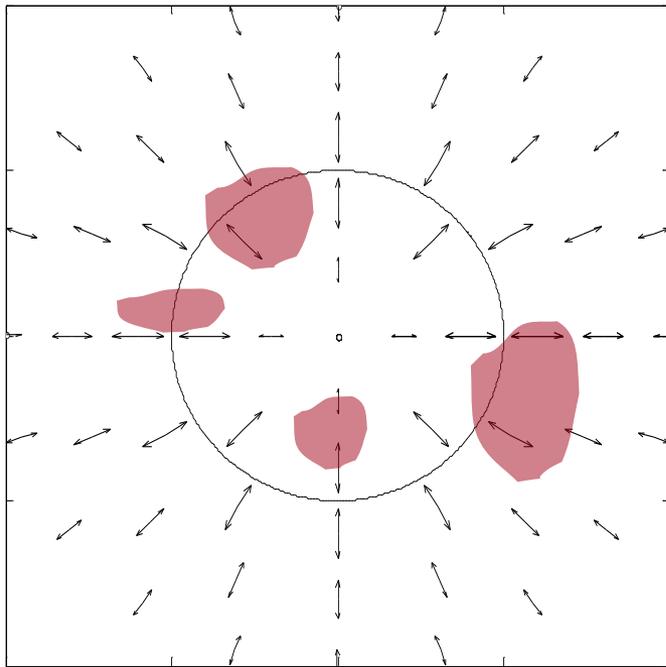
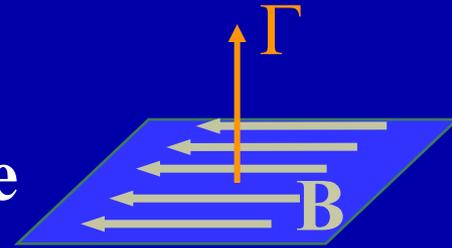
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Polarization in the observer frame

Random field
in shock plane



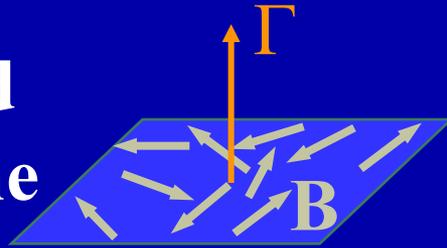
Ordered field
in shock plane



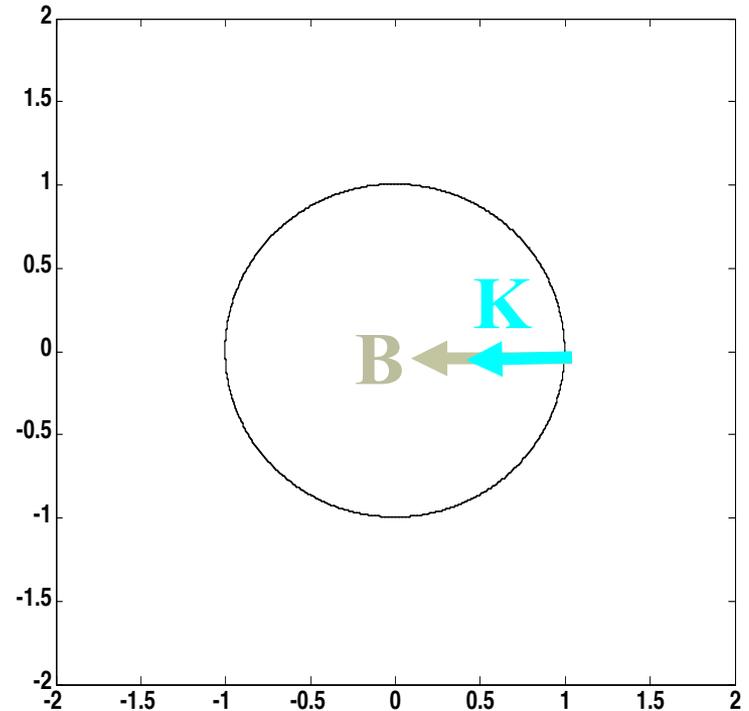
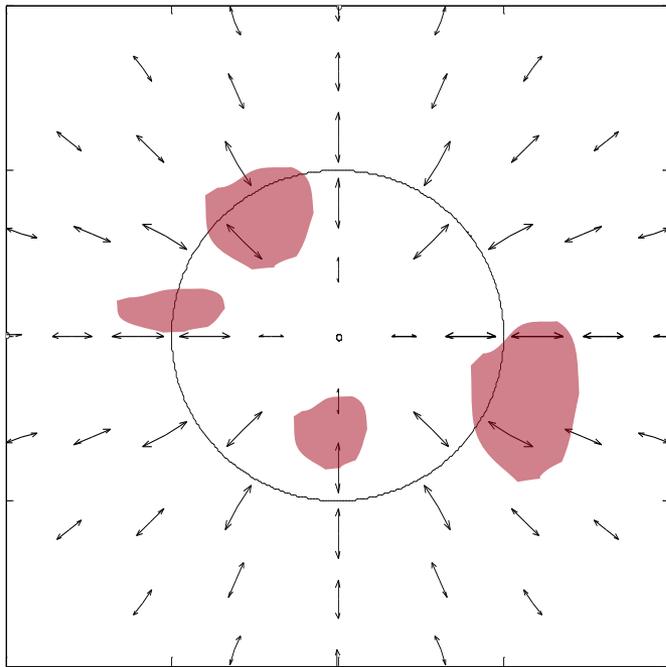
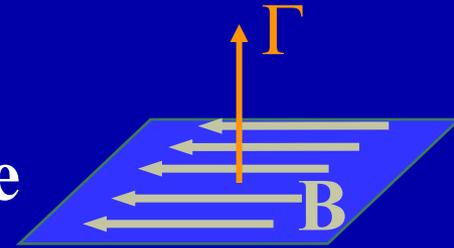
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Polarization in the observer frame

Random field
in shock plane



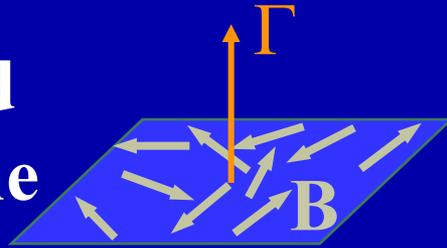
Ordered field
in shock plane



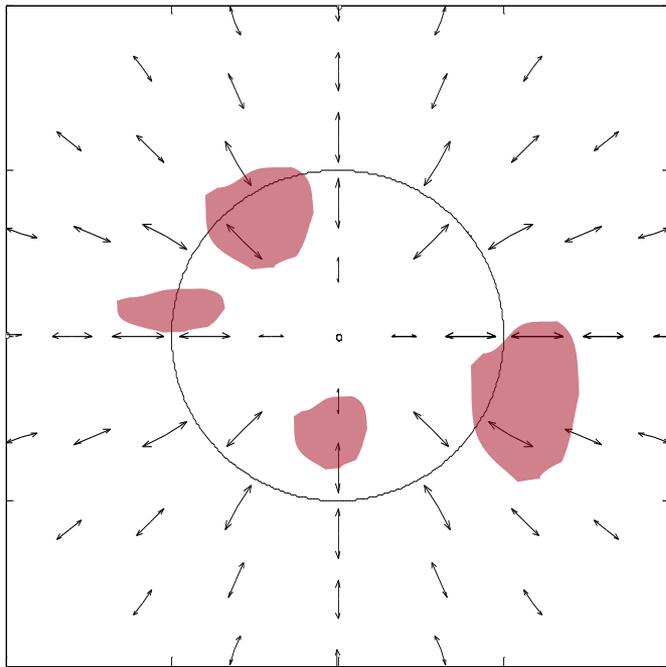
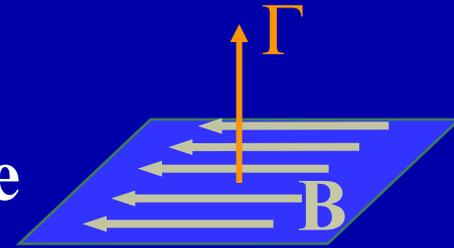
Sari 99; Ghisellini & Lazzati 99

Polarization in the observer frame

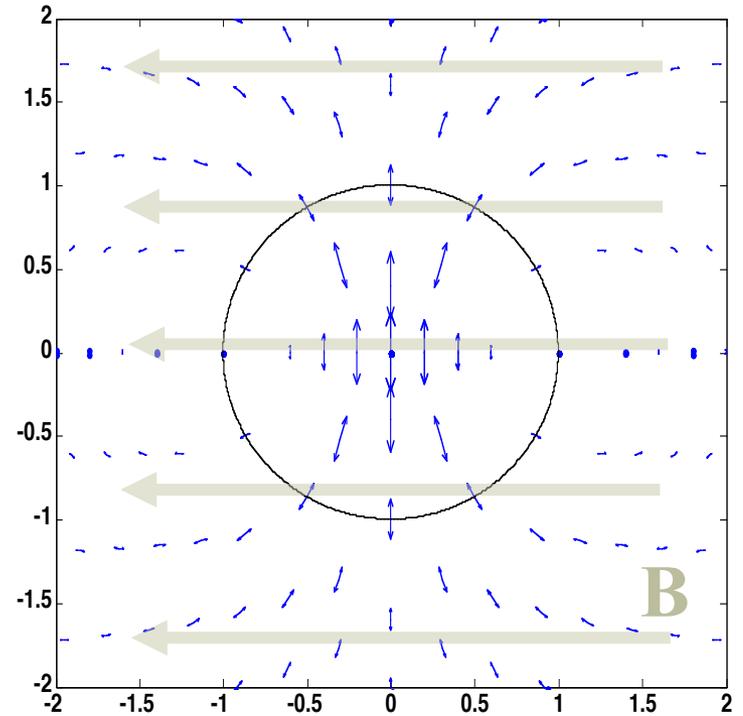
Random field
in shock plane



Ordered field
in shock plane



Sari 99; Ghisellini & Lazzati 99



Granot & Königl 03

$$P \sim P_{\max}$$

GRB Theoretical Framework:

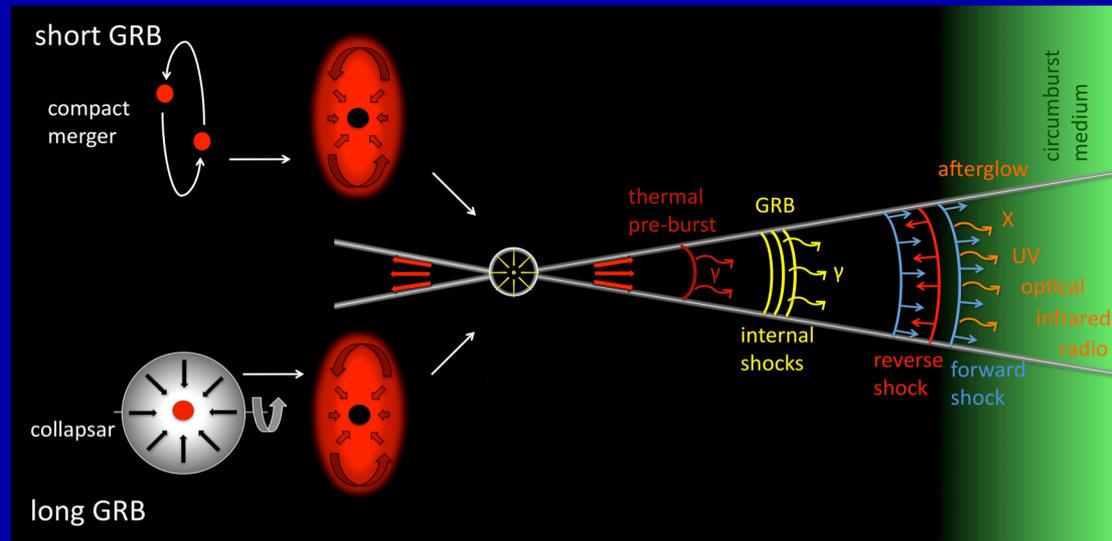
■ Progenitors:

◆ Short: binary mergers

◆ Long: massive stars

■ Jet Acceleration to

$\Gamma > 100$: P_{rad} / B-field?



■ **γ -rays**: dissipation: shocks/B? emission mechanism?

■ The jet **decelerates** as it sweeps up the external medium,

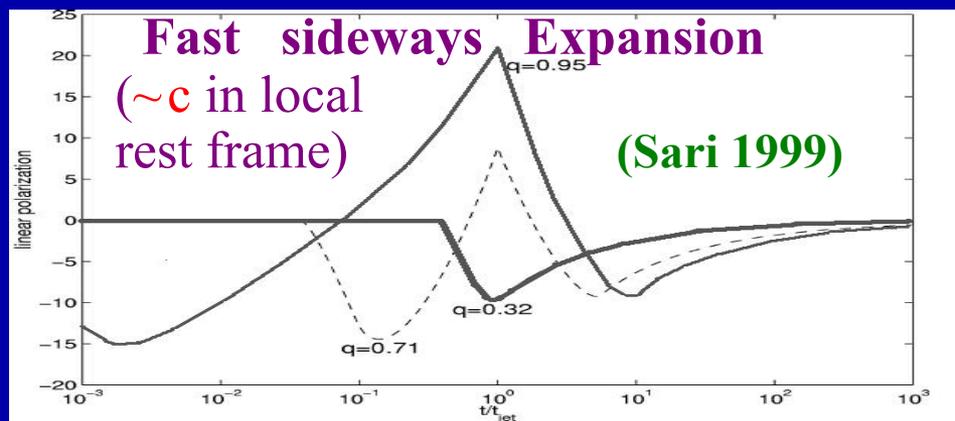
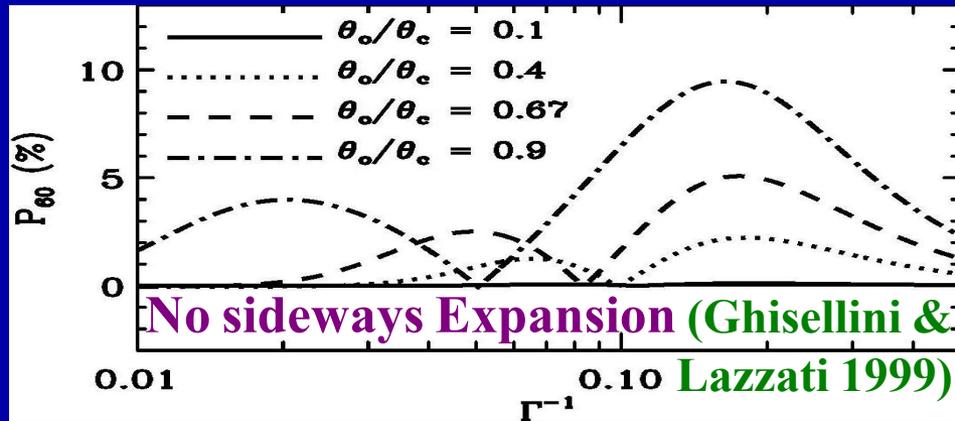
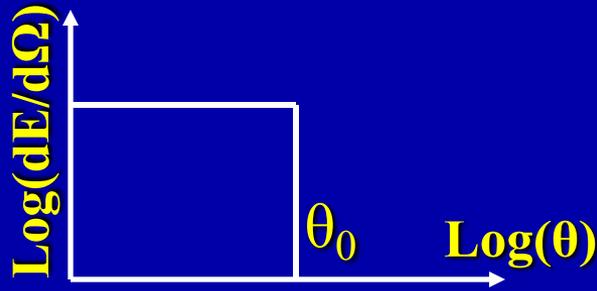
by a **reverse shock** (for $\sigma \lesssim 1$) \Rightarrow optical flash, radio flare

■ \Rightarrow **afterglow** from the long-lived forward shock going into the external medium: **X-ray** \rightarrow optical \rightarrow radio

Afterglow: Two “Traditional” Jet Structures

Uniform (top hat) jet:

(Rhoads 97,99;
Sari+99, ...)



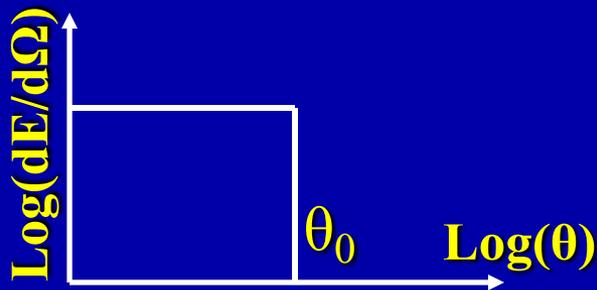
Main Prediction:
P vanishes & reappears
with θ_p rotated by 90°
Is not clearly observed

Also: $P \lesssim 10\%-20\%$
While $P_{\text{obs}} \sim 1-3\%$

Afterglow: Two “Traditional” Jet Structures

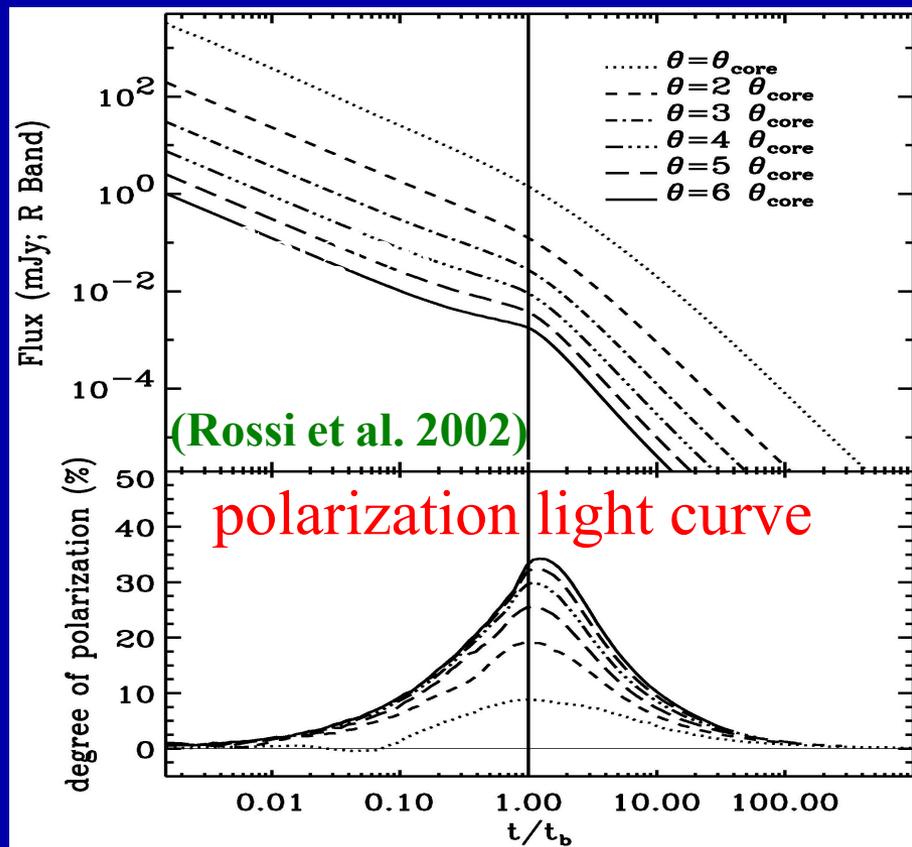
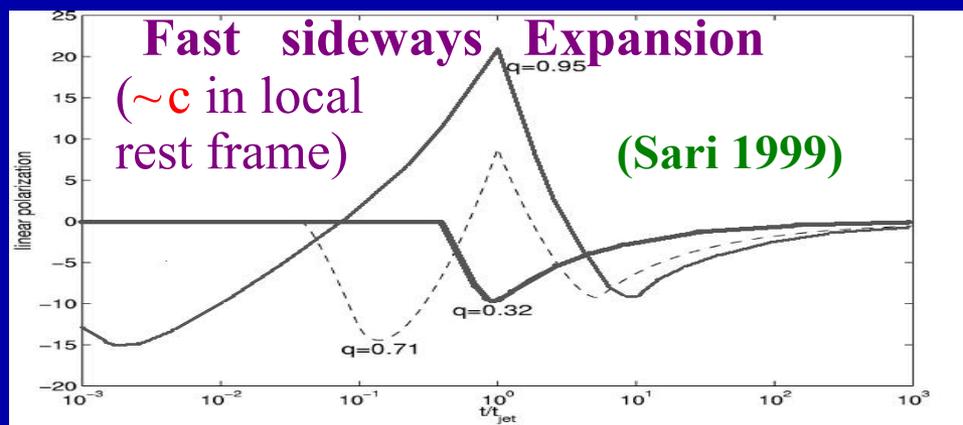
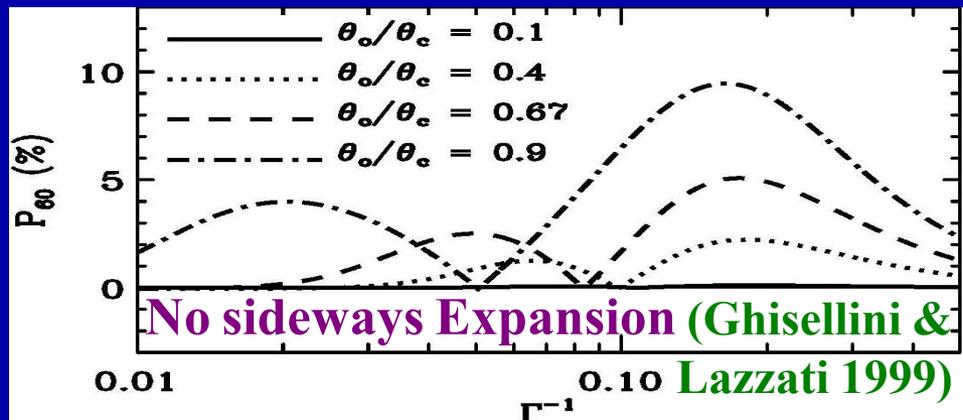
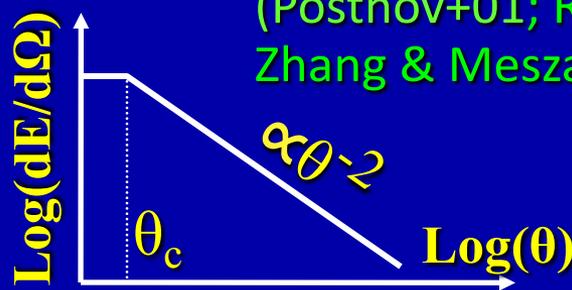
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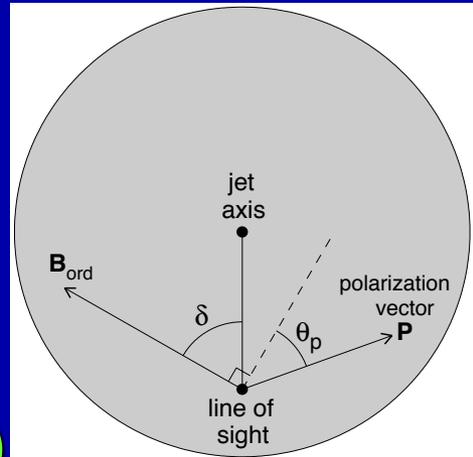
Structured jet:

(Postnov+01; Rossi+02;
Zhang & Meszaros 02)

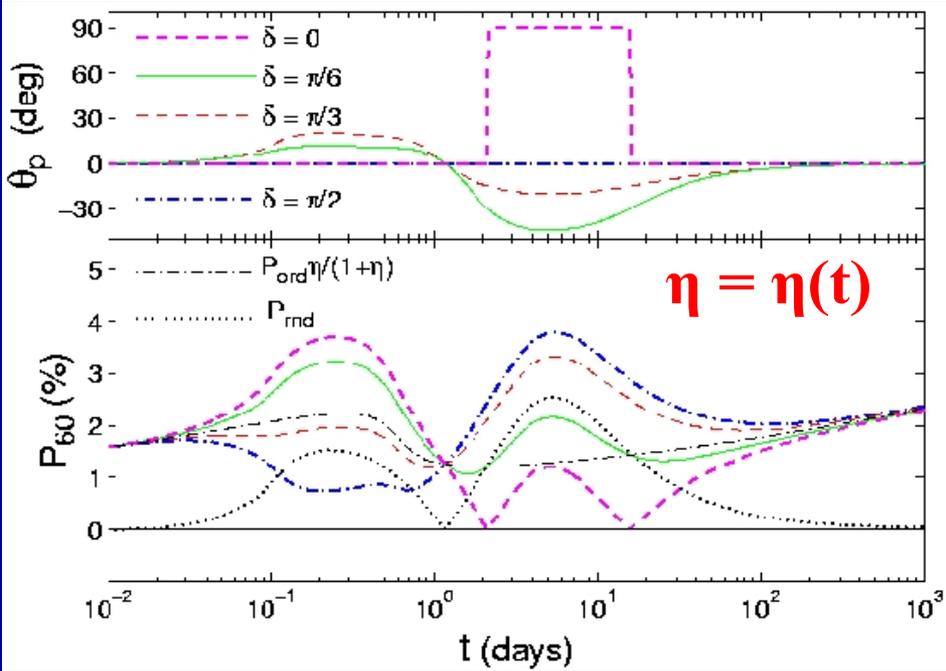
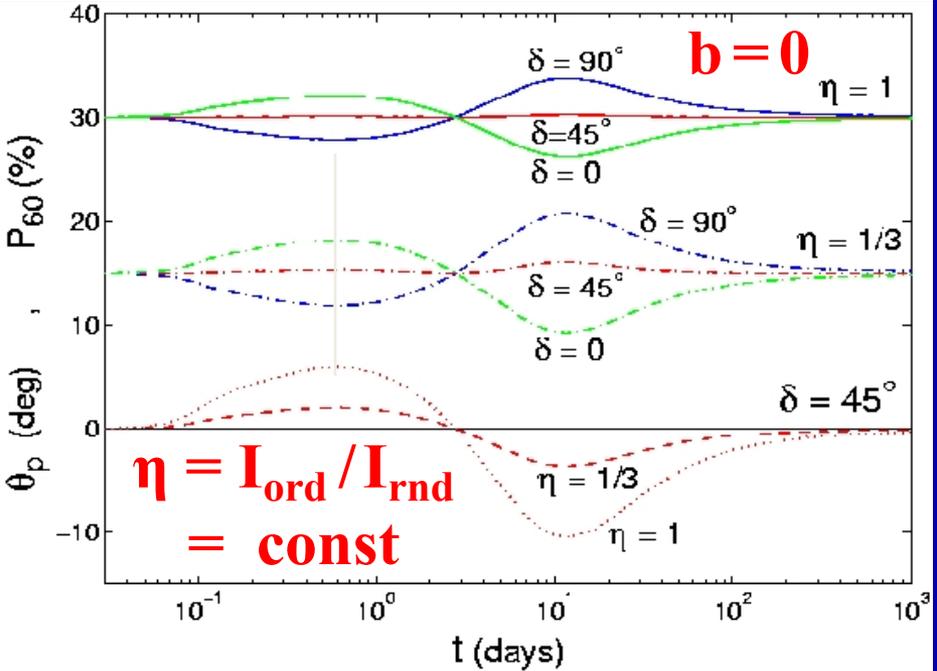


Combining Ordered B_{ord} & Random B_{rnd} Fields

- $P_{ord} \sim P_{max} \sim 60\%$ & $\theta_p = 90^\circ$ w.r.t. the direction of B_{ord}
- In the afterglow $P \lesssim 3\% \Rightarrow I_{ord} \ll I_{rnd}$ but we can still have $I_{ord}P_{ord} \gtrsim I_{rnd}P_{rnd}$
- $\Rightarrow B_{rnd}$ dominates I_{total} but B_{ord} dominates IP & P_{total}

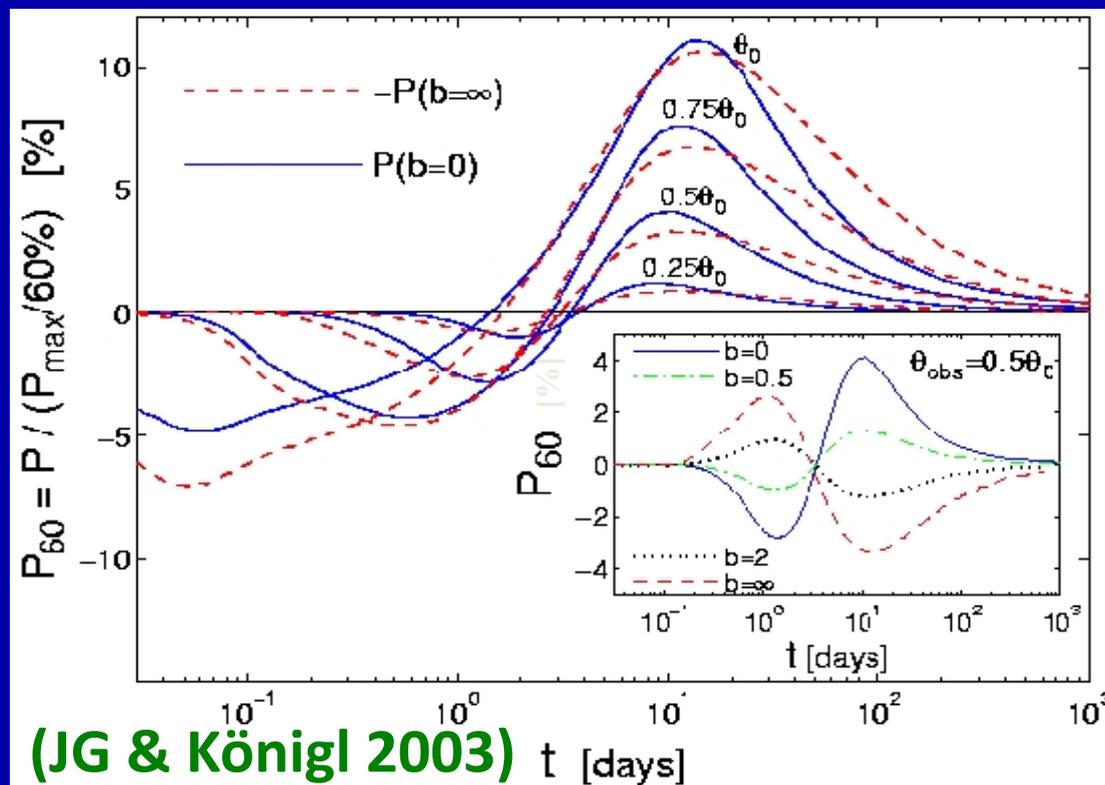


JG & Königl (2003)



The Random B-field's Degree of Anisotropy:

- $b = 2\langle B_{\parallel}^2 \rangle / \langle B_{\text{perp}}^2 \rangle$ parameterizes the asymmetry of \mathbf{B}_{rnd}
- $\text{Sign}(b-1)$ determines θ_p ($P > 0$ is along the direction from the line of sight to the jet axis & $P < 0$ is rotated by 90°)
- For $b \approx 1$ the polarization is very low (field is almost isotropic)
- $P \lesssim 3\%$ in afterglows observations $\Rightarrow 0.5 \lesssim b \lesssim 2$



$$P = P_{\text{max}} / [1 + 2 / (b-1) \sin^2 \theta']$$

(valid for $j'_v \propto [B' \sin \chi']^2$)

$$\theta_0 = 5^\circ$$

$$E_{\text{jet}} = 3 \times 10^{51} \text{ erg}$$

$$n = 1 \text{ cm}^{-3}$$

$$z = 1$$

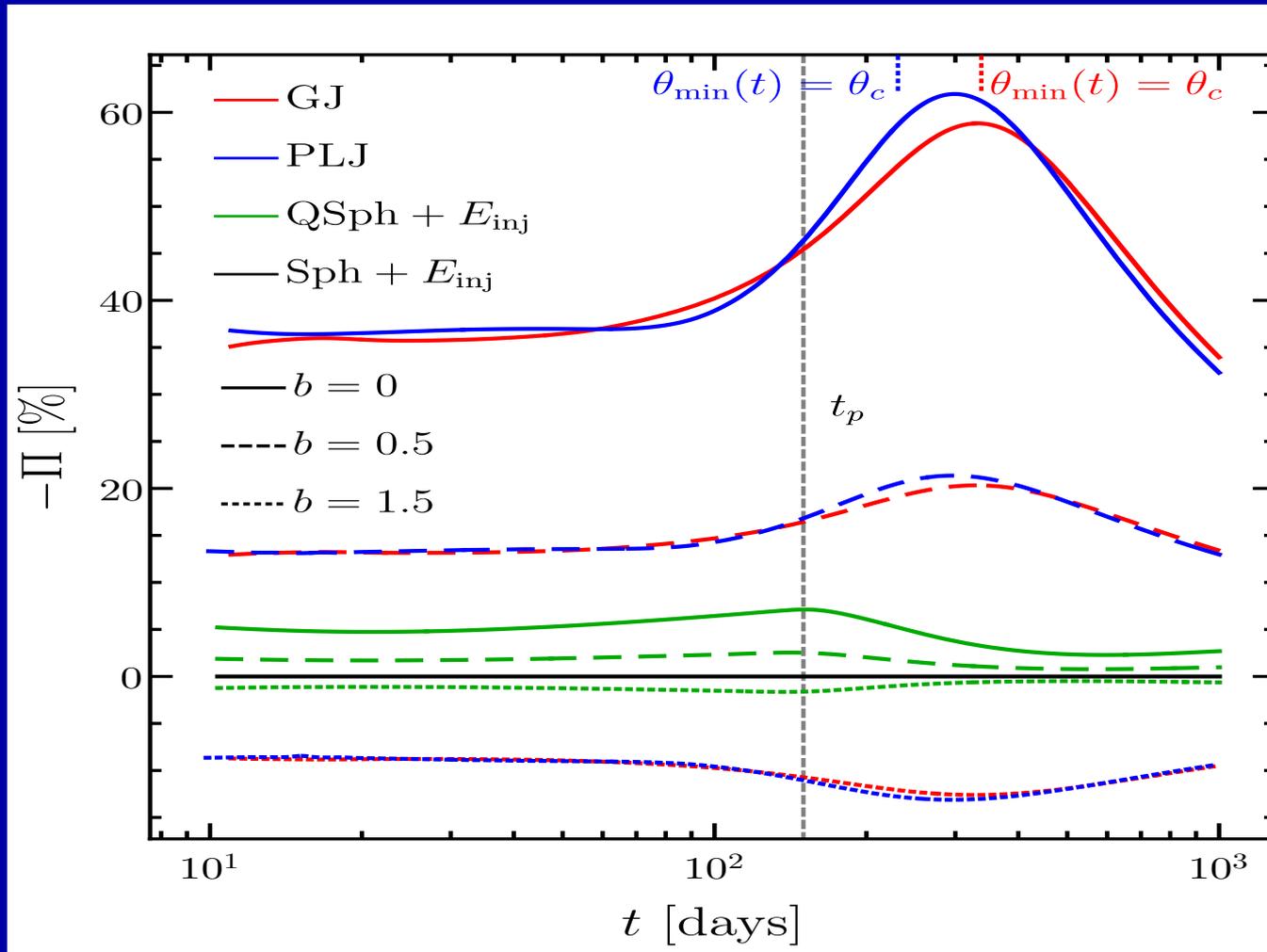
$$p = 2.5$$

$$\epsilon_e = 0.1$$

$$\epsilon_B = 0.01$$

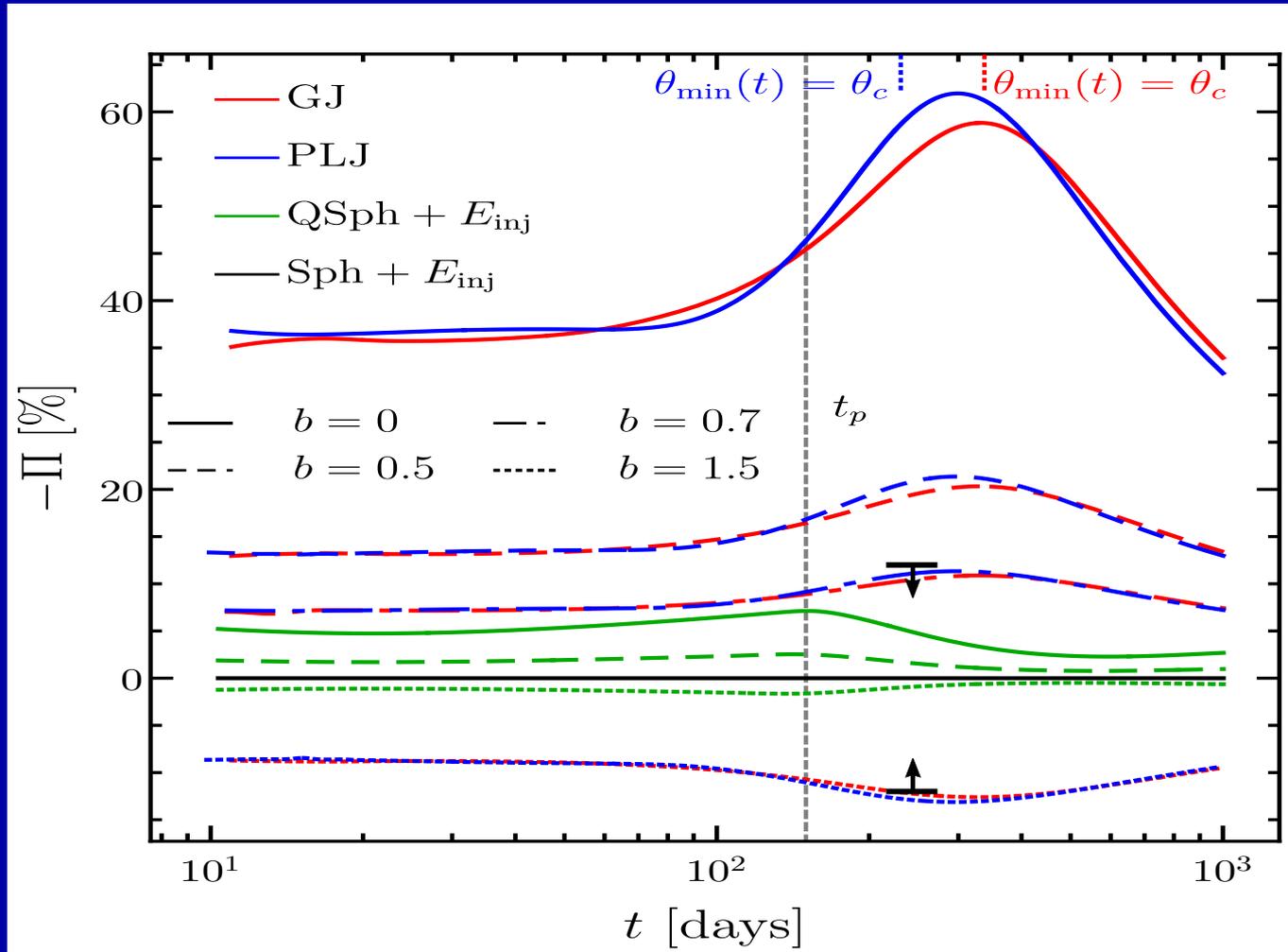
GW170817/GRB170817A Afterglow (Gill & JG 18)

- Assuming a shock-produced B-field with $b \equiv 2\langle B_{\parallel}^2 \rangle / \langle B_{\perp}^2 \rangle$
- Data favor two core-dominated jet models with similar $P(t)$



GW170817/GRB170817A Afterglow (Gill & JG 18)

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- Data favor two core-dominated jet models with similar $P(t)$



$0.66 \lesssim b \lesssim 1.49$
for jet models



New: upper limit
 $P_{\text{lin}} < 12\%$ @
 $\nu = 2.8 \text{ GHz}$,
 $t = 244 \text{ days}$
(Corsi + 2018)

GW170817/GRB170817A Afterglow (Gill & JG 19)

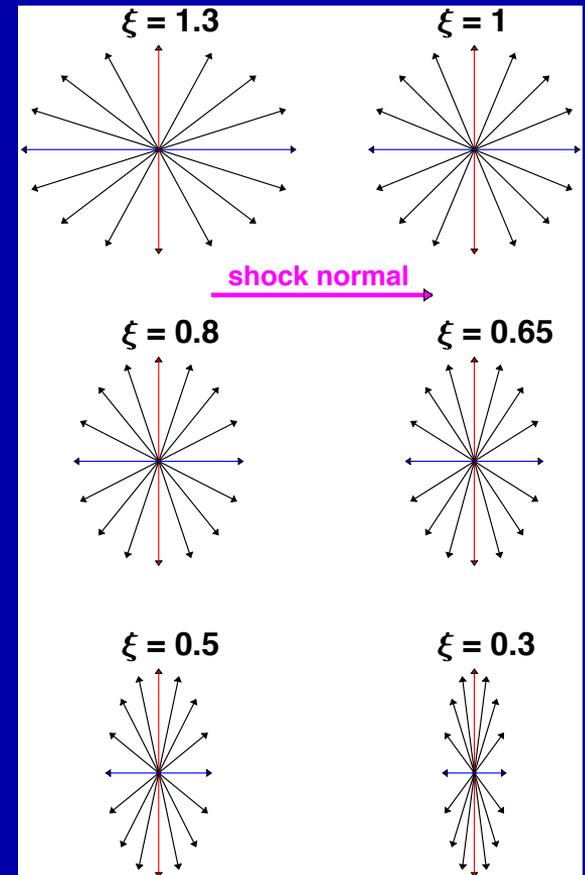
More realistic assumptions \Rightarrow B-field in collisionless shocks:

- 2D emitting shell \rightarrow 3D emitting volume (local BM76 radial profile)

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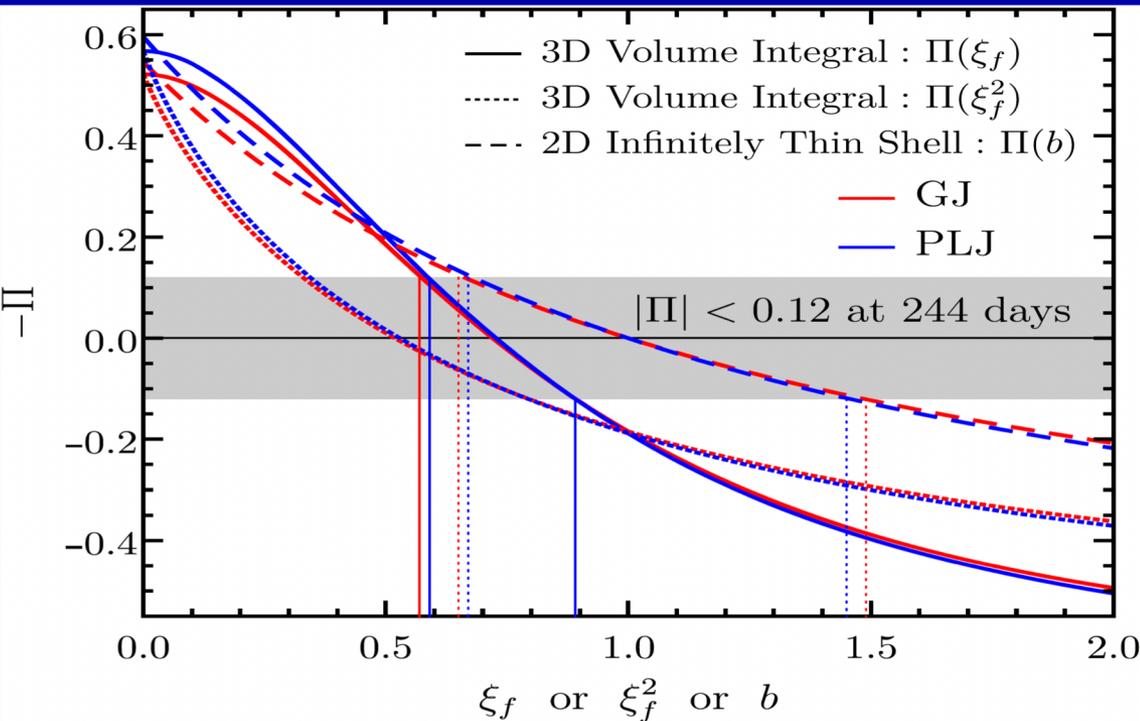
- 2D emitting shell \rightarrow 3D emitting volume (local BM76 radial profile)
- B-field evolution by faster radial expansion: $L'_r/L'_{\theta,\phi} \propto \chi^{(7-2k)/(8-2k)}$
B-field isotropic in 3D with $B'_r \rightarrow \xi B'_r$ (Sari 1999); $\xi = \xi_f \chi^{(7-2k)/(8-2k)}$



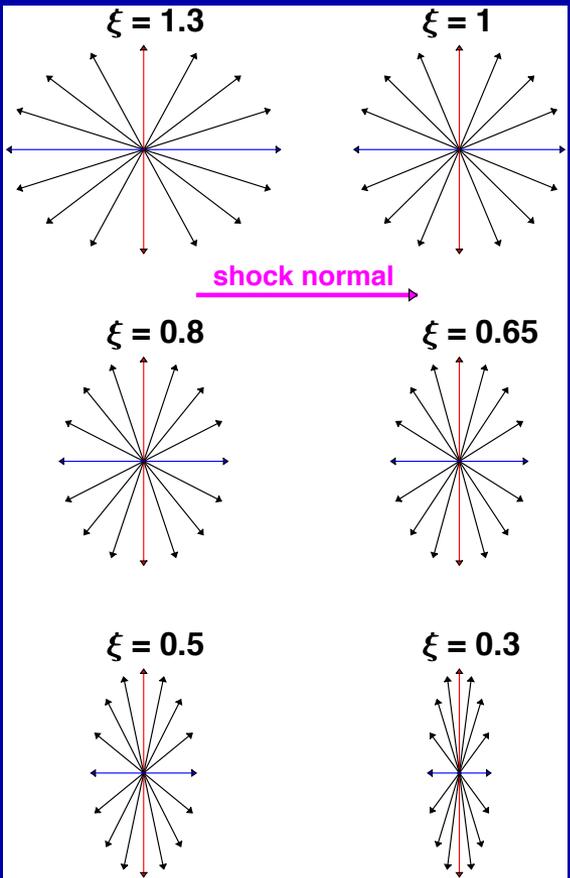
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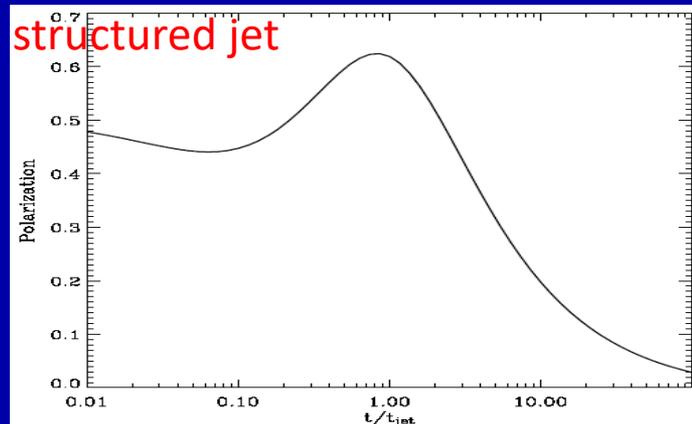


$0.57 \lesssim \xi_f \lesssim 0.89$

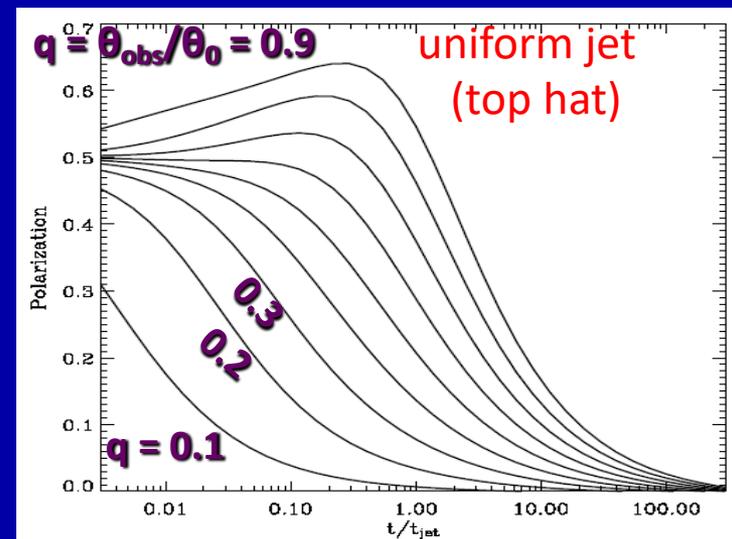


Reverse shock Pol.: B-field in ejecta

- The existence of a reverse shock $\Rightarrow \mathbf{E}_{EM} \lesssim \mathbf{E}_{kin} (\sigma \lesssim 1)$
- In the ‘optical flash’ the pol. should be similar to that in γ -rays, but much easier to measure & more reliable
- If \mathbf{B}_{ord} in the ejecta is ordered on angles $1/\Gamma_0 \lesssim \theta_B < \theta_j$ then $P \approx P_{max} \times \min(1, \Gamma\theta_B)$ due to averaging over $N \sim (\Gamma\theta_B)^{-2}$ incoherent patches (Granot & Königl 03) \Rightarrow smaller P & different θ_p in the ‘radio flare’ ($\Gamma \sim 10$)
- Toroidal B-field in the ejecta:



(Lazzati et al. 2004)



B-field	Optical Flash	Radio Flare ($t \sim t_j$)
Shock Produced	$\theta_{\text{obs}} \lesssim \theta_j - 1/\Gamma: P \approx 0$ $\theta_{\text{obs}} \sim \theta_j + 1/\Gamma: P \lesssim 50\%$	pol. due to jet structure \Rightarrow similar to afterglow
Uniform	$P \sim P_{\text{max}}$	$P \sim P_{\text{max}}$
Patches (θ_B)	$\theta_B \gtrsim 1/\Gamma_0: P \sim P_{\text{max}}$	$P \sim P_{\text{max}} \times \min(1, \Gamma\theta_B)$
Toroidal	$1/\Gamma_0 \lesssim \theta_{\text{obs}} \lesssim \theta_j:$ $P \sim P_{\text{max}}$	structured jet: $P \sim P_{\text{max}}$ top hat: $P \sim P_{\text{max}} (\theta_{\text{obs}}/\theta_j)^2$

Upper Limits on Polarization of Radio Flare Emission (Granot & Taylor 2005)

GRB	t (days)	t_j (days)	Π_L (3 σ)	Π_C (3 σ)
990123	1.25	≈ 2	< 23%	< 32%
991216	1.49	~ 2	< 11%	< 17%
	2.68		< 9%	< 15%
	1.49, 2.68		< 7%	< 9%
020405	1.19	~ 1-2	< 11%	< 19%

- Probably almost no depolarization in the host galaxy
- Likely no significant depolarization in the source due to different amounts of Faraday rotation; hard to rule out

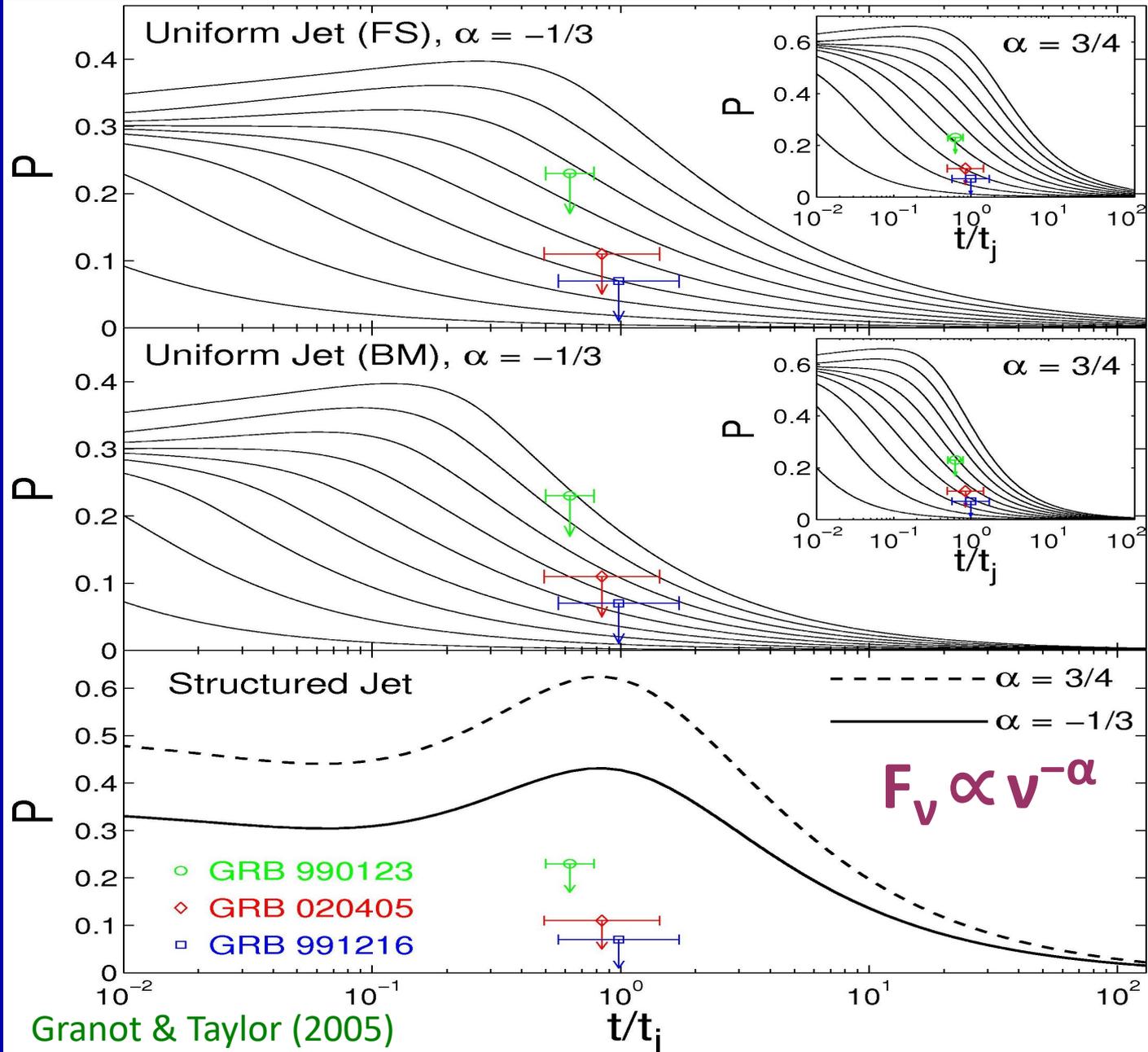
Toroidal Magnetic Field:

Dynamics of the Ejecta:

$\Gamma(t)$ follows that of the forward shock

$\Gamma(t)$ follows the Blandford & McKee self similar solution

$\Gamma(t)$ follows that of the forward shock



Implications of the Upper limits on the Radio Flare Polarization

B-field structure	Theoretical prediction	Theory vs. Observation
Shock Produced	pol. due to jet structure ⇒ similar to afterglow	✓
Uniform	$P \sim P_{\max}$	X
Patches (θ_B)	$P \sim P_{\max} \times \min(1, \Gamma \theta_B)$	$\theta_B \lesssim P_{\lim} / \Gamma P_{\max} \sim 10^{-2}$
Toroidal	structured jet: $P \sim P_{\max}$ tophat: $P \sim P_{\max} (\theta_{\text{obs}} / \theta_j)^2$	X $\theta_{\text{obs}} / \theta_j \lesssim 0.4 - 0.55$

Implications of the Upper limits on the Radio Flare Polarization

New Results: Tanmoy Laskar's talk

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Prompt γ -ray Polarization: hard to measure

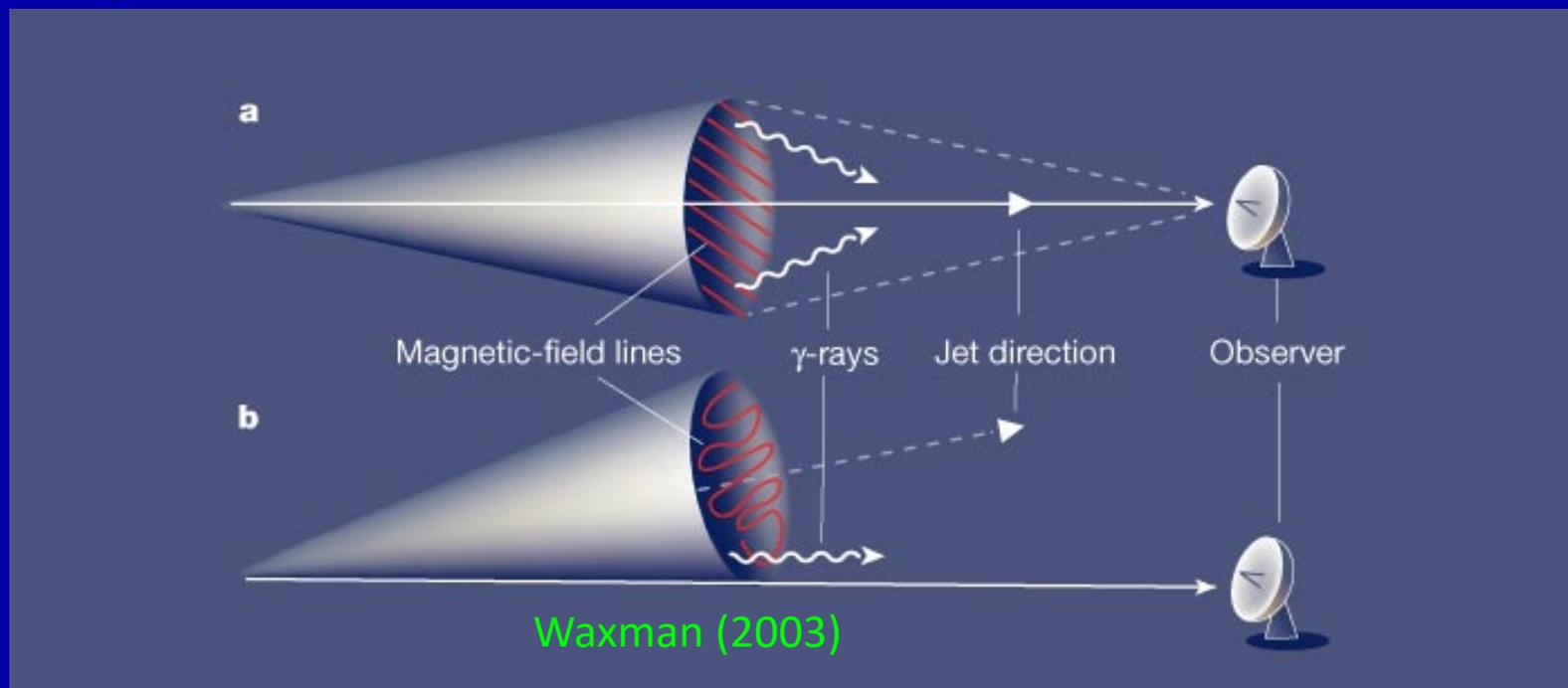
First consider synchrotron emission:

■ Shock produced B-field + $\theta_{\text{obs}} \lesssim \theta_j - 1/\Gamma \Rightarrow P \approx 0$

■ $P \sim P_{\text{max}}$ can be achieved in the following ways:

(1) **ordered magnetic field** in the ejecta,

(2) **special geometry**: $|\theta_{\text{obs}} - \theta_j| \lesssim 1/\Gamma \Rightarrow$ favors narrow jets: $\theta_j \lesssim 1/\Gamma$ (works with a shock produced B-field)



Narrow Jet + shock produced B-field

- High polarization + reasonable flux $\Rightarrow \theta_j < \theta_{\text{obs}} \lesssim \theta_j + 1/\Gamma$
- A reasonable probability for such $\theta_{\text{obs}} \Rightarrow \Gamma\theta_j \lesssim \text{a few}$
- Since $\Gamma \gtrsim 100$ & $\theta_j \gtrsim 0.05$, $\Gamma\theta_j \gtrsim 5$ and is typically larger

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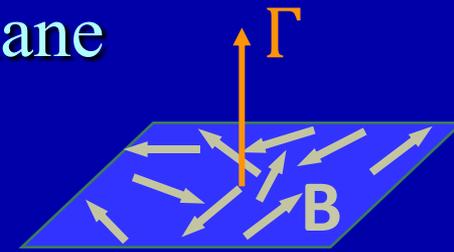
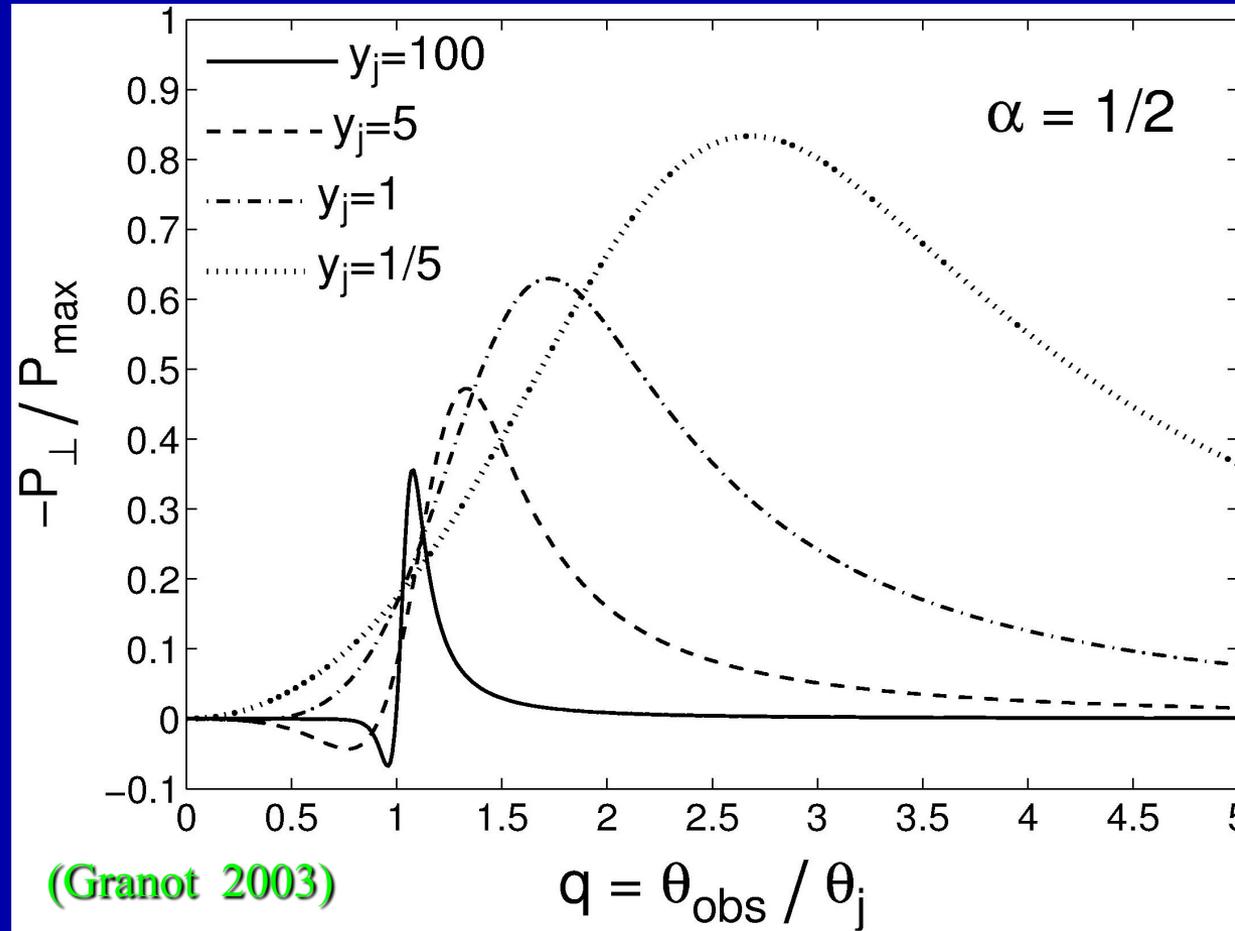
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- Afterglow obs. imply more random B_{rnd} : $0.57 \lesssim \xi_f \lesssim 0.89$

Adding pulses: Random B-field in shock plane



$$y_j = (\Gamma \theta_j)^2$$

$$F_{\nu} \propto \nu^{-\alpha}$$

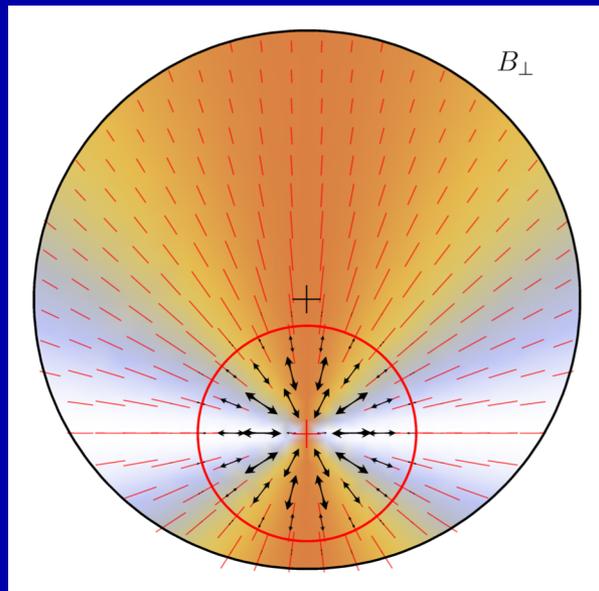
- $\Delta\Gamma \sim \Gamma$ between different shell collisions (different pulses in GRB light curve) reduces \mathbf{P} by a factor ~ 2

Prompt γ -ray Polarization: short summary

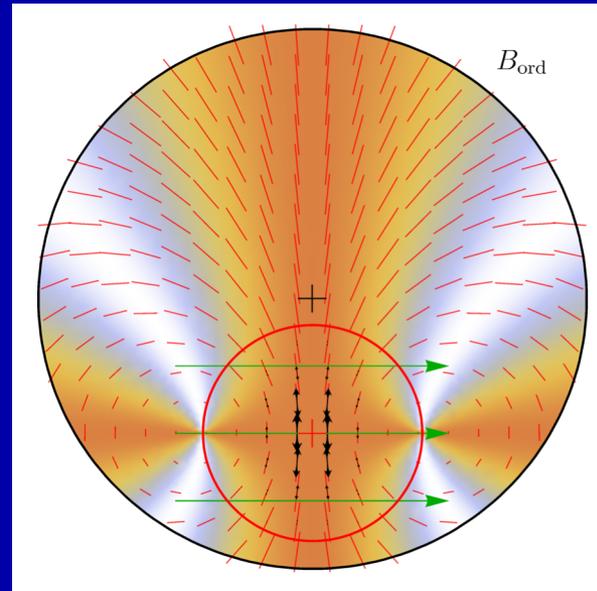
	Ordered Field	Sharp-edge Jet
$P \sim 80\%$	X	X
$P \sim 50\%$	✓	X
$P \sim 25\%$	with $B_{\text{rnd}} \lesssim B_{\text{ord}}$	✓
$P \lesssim 10\%$	$B_{\text{rnd}} > B_{\text{ord}}$	with $B_{\text{rnd}} \gtrsim B_{\text{ord}}$
statistics	High P in all GRBs	low P in most GRBs
Potential problems	Some B_{rnd} required for Fermi acceleration	$\Gamma\theta_j \lesssim \text{a few}, \Delta\Gamma \sim \Gamma,$ $B_{\text{rnd}} (0.57 \lesssim \xi_f \lesssim 0.89)$ $\Delta\theta_j \lesssim 1/4\Gamma$

Prompt GRB Polarization (Gill, JG & Kumar 2020):

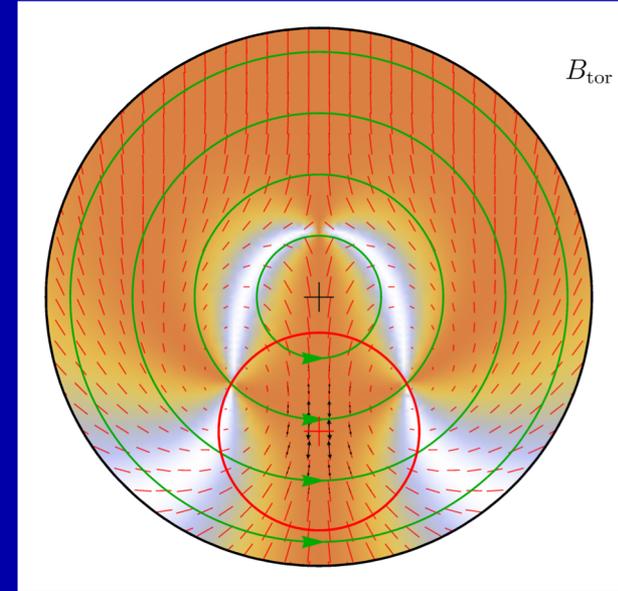
- Comprehensive study in view of γ -ray polarimetry missions
- Jet structure: top hat (sharp/smooth), Gaussian, core+power-law
- Emission mechanism: **synchrotron**, photospheric, Compton drag
- Time integrated over single or multiple pulses



Random B-field in 2D



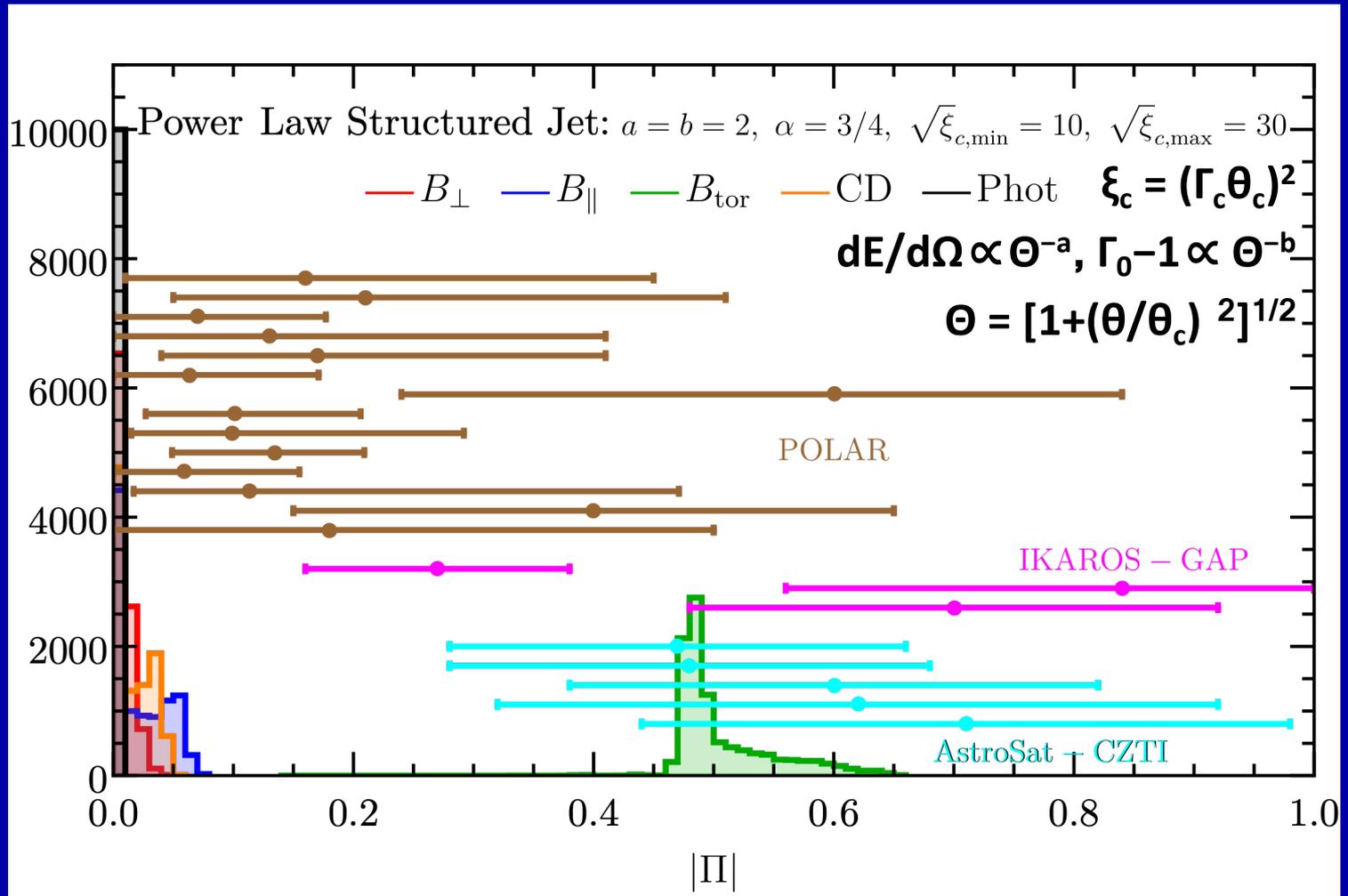
Ordered B-field



Toroidal B-field

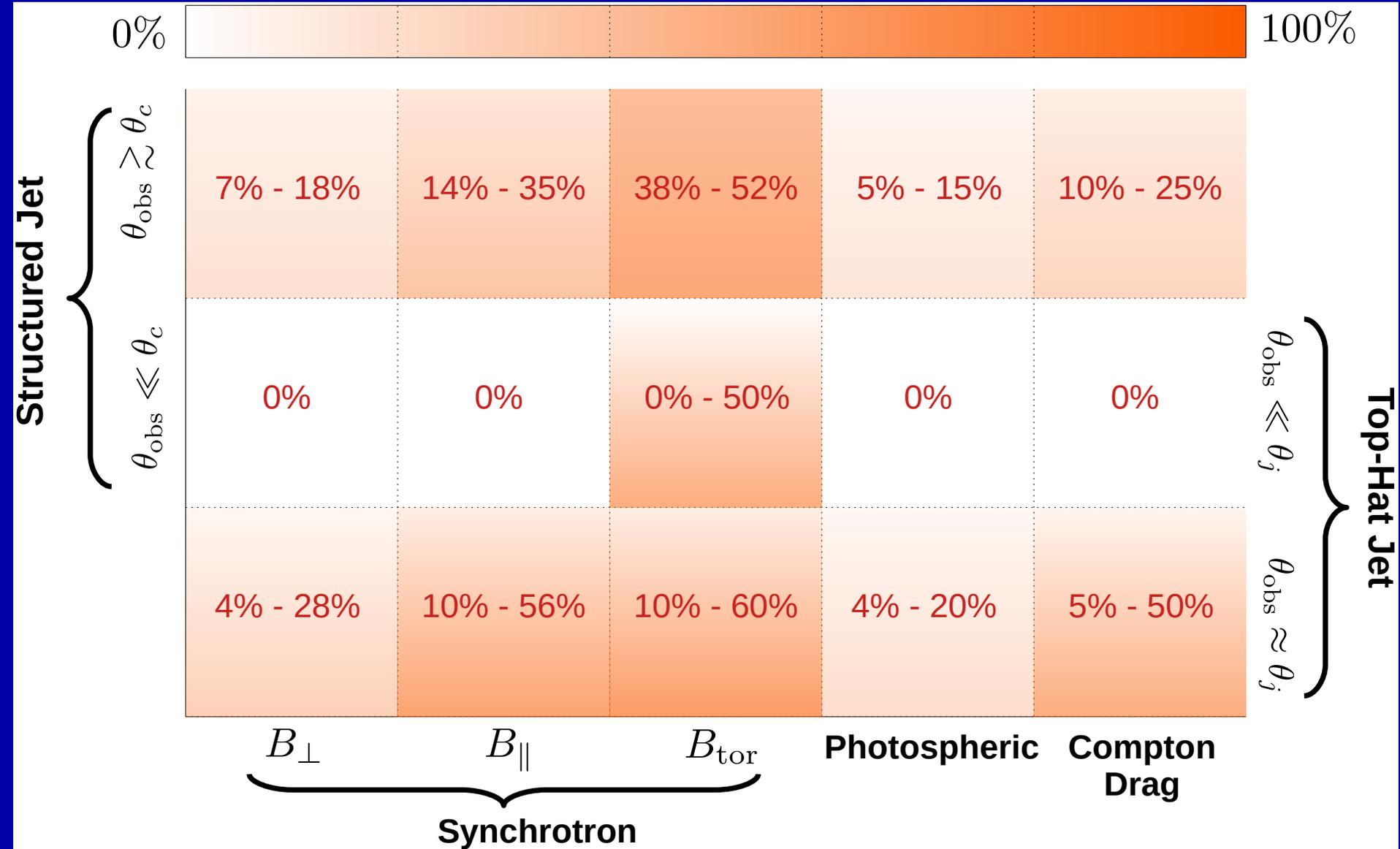
Prompt GRB Polarization (Gill, JG & Kumar 2018):

- Model comparison: structured jet, integrating 10 pulses



- $B_{\text{tor}}/B_{\text{ord}}$ is favored if $P \sim 50\text{-}65\%$ in 1 ($\geq 20\%$ in most) GRBs

Prompt GRB Polarization (Gill, Kole & JG 2022):



Conclusions:

- **Afterglow polarization** probes jet structure & dynamics + the B-field structure behind relativistic collisionless shocks
- ◆ \Rightarrow GW170817: $0.57 < \xi_0 < 0.89$ (B_{rd}) + core-dominated jet
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- Reverse shock polarization probes B-field structure in ejecta
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 - ◆ Optical / Radio results: talks by Jordana-Mitjans / Laskar

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 - ◆ Optical / Radio results: talks by Jordana-Mitjans / Laskar
- Prompt GRB pol. probes emission mechanism & jet structure
 - ◆ Observations are improving & new planned missions
 - ◆ Theory is improving to match the upcoming observations
 - ◆ $B_{\text{ord}}/B_{\text{tor}}$ favored if $P \sim 50\text{-}65\%$ in 1 ($\gtrsim 20\%$ in most) GRBs
(talks by Kole, Gill, Parsotan, De Angelis)